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The Bond Premium in a DSGE Model with Long-Run Real and Nominal Risks

Glenn D. Rudebusch Eric T. Swanson

Economic Research Federal Reserve Bank of San Francisco

Conference on Monetary Policy and Financial Markets National Bank of Belgium October 16, 2008 DSGE Model with EZ Preferences

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3 Long-Run Risks



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Why Study Asset Prices in a DSGE Model?

Asset pricing is important:

- DSGE models increasingly used for policy analysis; total failure to explain asset prices may signal flaws in the model
- many empirical questions about asset prices require a structural DSGE model to provide reliable answers

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Equity prices have received much attention in the literature But bond prices are at least as interesting because they:

- apply to a larger amount of securities
- provide an additional perspective on the model
- test nominal rigidities in the model
- model short-term interest rate process, not dividends

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The Bond Premium Puzzle

The equity premium puzzle: excess returns on stocks are much larger (and more variable) than can be explained by standard preferences in an RBC model (Mehra and Prescott, 1985).

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The bond premium puzzle: excess returns on long-term bonds are much larger (and more variable) than can be explained by standard preferences in an RBC model (Backus, Gregory, and Zin, 1989).

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The bond premium puzzle: excess returns on long-term bonds are much larger (and more variable) than can be explained by standard preferences in an RBC model (Backus, Gregory, and Zin, 1989).

Note:

• Since Backus, Gregory, and Zin (1989), DSGE models with nominal rigidities have advanced considerably

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Recent Studies of the Bond Premium Puzzle

- Wachter (2005)
 - can resolve bond premium puzzle using Campbell-Cochrane preferences in endowment economy

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 - can resolve bond premium puzzle using Epstein-Zin preferences in endowment economy

We examine to what extent the Piazzesi-Schneider results generalize to the DSGE model and a production economy

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Our Analysis

We incorporate Epstein-Zin preferences in standard DSGE model

The model has three key ingredients:

- Intrinsic nominal rigidities
 - makes bond pricing interesting
- Epstein-Zin preferences
 - makes households risk averse
- Long-run risk (productivity or inflation)
 - introduces a risk households cannot offset
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Can we match the unconditional moments of both bond prices and macroeconomic variables?

Conclusions

Related Strands of the Literature

The Bond Premium in a DSGE Model:

 Backus, Gregory, Zin (1989), Donaldson, Johnson, Mehra (1990), Den Haan (1995), Doh (2006), Rudebusch, Swanson (2008)

Epstein-Zin Preferences and the Bond Premium in an Endowment Economy:

 Piazzesi, Schneider (2006), Colacito, Croce (2007), Backus, Routledge, Zin (2007), Gallmeyer, Hollifield, Palomino, Zin (2007), Bansal, Shaliastovich (2008), Doh (2008)

Epstein-Zin Preferences in a DSGE Model:

 Tallarini (2000), Croce (2007), Levin, Lopez, Salido, Nelson, Yun (2008)

Epstein-Zin Preferences and the Bond Premium in a DSGE Model:

 van Binsbergen, Fernandez-Villaverde, Koijen, Rubio-Ramirez (2008)

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A DSGE Model with Epstein-Zin Preferences



A DSGE Model with Epstein-Zin Preferences

- Standard Preferences
- Epstein-Zin Preferences
- Firms and Government
- Bond Pricing and Measures of the Bond Premium
- Results

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Standard Preferences

Representative household with preferences:

$$\max E_t \sum_{t=0}^{\infty} \beta^t \left(\frac{(c_t - h_t)^{1-\gamma}}{1-\gamma} - \chi_0 \frac{l_t^{1+\chi}}{1+\chi} \right)$$

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Stochastic discount factor (nominal):

$$m_{t+1} = \frac{\beta (C_{t+1} - bC_t)^{-\gamma}}{(C_t - bC_{t-1})^{-\gamma}} \frac{P_t}{P_{t+1}}$$

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Parameters: $\beta = .99$, b = .66, $\gamma = 2$, $\chi = 1.5$

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Epstein-Zin Preferences

Standard preferences:

$$V_t \equiv u(c_t, I_t) + \beta E_t V_{t+1}$$

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We'll use standard NK utility kernel:

$$u(c_t, l_t) \equiv \frac{c_t^{1-\gamma}}{1-\gamma} - \chi_0 \frac{l_t^{1+\chi}}{1+\chi}$$

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$$u(c_t, l_t) \equiv \frac{c_t^{1-\gamma}}{1-\gamma} - \chi_0 \frac{l_t^{1+\chi}}{1+\chi}$$

Epstein-Zin stochastic discount factor (nominal):

$$m_{t,t+1} \equiv \frac{\beta u_1 \big|_{(c_{t+1},l_{t+1})}}{u_1 \big|_{(c_t,l_t)}} \left(\frac{V_{t+1}}{(E_t V_{t+1}^{1-\alpha})^{1/(1-\alpha)}} \right)^{\alpha} \frac{P_t}{P_{t+1}}$$

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Firms and Government

Continuum of differentiated firms:

- face Dixit-Stiglitz demand with elasticity $\frac{1+\theta}{\theta}$, markup θ
- set prices in Calvo contracts with avg. duration 4 quarters
- identical production functions: $y_t = A_t \bar{k}^{1-\eta} I_t^{\eta}$
- have firm-specific capital stocks
- face aggregate technology: $\log A_t = \rho_A \log A_{t-1} + \varepsilon_t^A$

Parameters $\theta = .2$, $\rho_A = .9$, $\sigma_A^2 = .01^2$

Perfectly competitive goods aggregation sector

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Firms and Government

Government:

- imposes lump-sum taxes G_t on households
- destroys the resources it collects

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$$\log G_t = \rho_G \log G_{t-1} + (1 - \rho_g) \log \overline{G} + \varepsilon_t^G$$

Parameters $\bar{G} = .17 \bar{Y}$, $\rho_G = .9$, $\sigma_G^2 = .004^2$

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$$\log G_t = \rho_G \log G_{t-1} + (1 - \rho_g) \log \overline{G} + \varepsilon_t^G$$

Parameters $\bar{G} = .17 \bar{Y}$, $\rho_G = .9$, $\sigma_G^2 = .004^2$

Monetary Authority:

$$i_t = \rho_i i_{t-1} + (1 - \rho_i) [1/\beta + \pi_t + g_y(y_t - \bar{y}) + g_\pi(\bar{\pi}_t - \pi^*)] + \varepsilon_t^i$$

Parameters $\rho_i = .73$, $g_y = .53$, $g_{\pi} = .93$, $\pi^* = 0$, $\sigma_i^2 = .004^2$

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Bond Pricing

Pricing of any nominal asset:

 $p_t = d_t + E_t[m_{t+1}p_{t+1}]$



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Bond Pricing

Pricing of any nominal asset:

$$p_t = d_t + E_t[m_{t+1}p_{t+1}]$$

Zero-coupon nominal bond pricing:

$$p_t^{(n)} = E_t[m_{t+1}p_{t+1}^{(n-1)}]$$
$$i_t^{(n)} = -\frac{1}{n}\log p_t^{(n)}$$

Notation: let $i_t \equiv i_t^{(1)}$

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The Term Premium

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The Term P	remium		

In DSGE framework, convenient to work with a default-free *consol*, a perpetuity that pays \$1, δ_c , δ_c^2 , δ_c^3 , ... (nominal)

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Price of the consol:

$$\widetilde{p}_t^{(n)} = 1 + \delta_c \, E_t m_{t+1} \widetilde{p}_{t+1}^{(n)}$$

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Risk-neutral consol price:

$$\widehat{p}_t^{(n)} = 1 + \delta_c \, e^{-i_t} E_t \widehat{p}_{t+1}^{(n)}$$

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Term premium:

$$\psi_t^{(n)} \equiv \log\left(\frac{\delta_c \widetilde{p}_t^{(n)}}{\widetilde{p}_t^{(n)} - 1}\right) - \log\left(\frac{\delta_c \widehat{p}_t^{(n)}}{\widehat{p}_t^{(n)} - 1}\right)$$

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Solving the Model

We solve the model by perturbation methods

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We solve the model by perturbation methods

- In a first-order approximation, term premium is zero
- In a second-order approximation, term premium is a constant (sum of variances)
- So we compute a *third*-order approximation of the solution around nonstochastic steady state

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The model has a relatively large number of state variables: C_{t-1} , A_{t-1} , G_{t-1} , i_{t-1} , Δ_{t-1} , $\bar{\pi}_{t-1}$, ε_t^A , ε_t^G , ε_t^i . It is difficult to solve, impossible to estimate

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It is difficult to solve, impossible to estimate

We examine unconditional moments of standard parameters We also search for over parameter space for the "best fit" set, which minimizes the average deviation of 13 moments

Definitions of Unconditional Moments Matched

Variable	U.S. Data, 1961-2007
sd[C]	Real consumption*
sd[<i>L</i>]	Labor, total hours worked*
sd[w ^r]	Real wage*
$sd[\pi]$	Price inflation, Annualized quarterly rate
sd[<i>i</i>]	Short-term nominal interest rate, annualized p.p.
sd[<i>r</i>]	Short-term real interest rate, annualized p.p.
sd[<i>i</i> ⁽¹⁰⁾]	10-year zero-coupon nominal rate, annualized p.p.
mean[$\psi^{(10)}$]	Term premium on 10-year zero-coupon bond
$sd[\psi^{(10)}]$	(affine no-arbitrage estimates)
mean[<i>i</i> ⁽¹⁰⁾ – <i>i</i>]	Yield curve slope
sd[<i>i</i> ⁽¹⁰⁾ - <i>i</i>]	(long - short rate, annualized p.p.)
mean[x ⁽¹⁰⁾]	Quarterly excess holding period return
sd[x ⁽¹⁰⁾]	(10-year bond, annualized p.p.)

*deviations from HP trend in percentage points

Table 2: Empirical and Model-Based Moments

	U.S. Data	EU	EZ	"best fit" EZ
variable	1961-2007	Preferences	Preferences	Preferences
sd[<i>C</i>]	1.19	1.42	1.45	2.53
sd[<i>L</i>]	1.71	2.56	2.50	2.21
sd[w ^r]	0.82	2.08	2.02	1.52
$sd[\pi]$	2.52	2.25	2.30	2.71
sd[<i>i</i>]	2.71	1.90	1.93	2.27
sd[<i>r</i>]	2.30	1.89	1.95	1.62
sd[<i>i</i> ⁽¹⁰⁾]	2.41	0.54	0.57	1.03
mean[$\psi^{(10)}$]	1.06	.010	.438	1.05
$sd[\psi^{(10)}]$	0.54	.000	.053	.184
mean[<i>i</i> ⁽¹⁰⁾ - <i>i</i>]	1.43	047	.390	0.99
sd[<i>i</i> ⁽¹⁰⁾ - <i>i</i>]	1.33	1.43	1.43	1.33
mean[x ⁽¹⁰⁾]	1.76	.015	.431	1.04
sd[x ⁽¹⁰⁾]	23.43	6.56	6.87	9.02
memo: IES		.5	.5	1.3
quasi-CRRA		2	75	75

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Coefficient of Relative Risk Aversion

In a standard DSGE model:

- additive labor implies utility kernel is nonhomothetic
- shocks are not multiplicative with respect to wealth
- wealth includes human capital as well as physical capital

Conclusions

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Coefficient of Relative Risk Aversion

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For lack of a better measure, we report the quasi-CRRA, $1 - (1 - \gamma)(1 - \alpha)$

This is the CRRA *if* labor were held fixed and *if* all shocks were multiplicative with respect to wealth

Conclusions

Coefficient of Relative Risk Aversion

In a standard DSGE model:

- additive labor implies utility kernel is nonhomothetic
- shocks are not multiplicative with respect to wealth
- wealth includes human capital as well as physical capital

For lack of a better measure, we report the quasi-CRRA, $1 - (1 - \gamma)(1 - \alpha)$

This is the CRRA *if* labor were held fixed and *if* all shocks were multiplicative with respect to wealth

Better measures of risk aversion (e.g., thought experiments) are likely to look less risk-averse than the quasi-CRRA would suggest

households can self-insure risk by varying labor supply

DSGE Model with EZ Preferences

Long-Run Risks

Conclusions

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Long-Run Risks

3 Long-Run Risks

- Long-Run Real Risk
- Long-Run Inflation Risk

DSGE Model with EZ Preferences

Long-Run Risks ●000000 Conclusions

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Long-Run Productivity Risk

Following Bansal and Yaron (2004), introduce long-run real risk to make the economy more risky:

Assume productivity follows:

$$\log A_t^* = \rho_{A^*} \log A_{t-1}^* + \varepsilon_t^{A^*}$$
$$\log A_t = \log A_t^* + \varepsilon_t^A$$
where $\rho_{A^*} = .98$, $\sigma_{A^*} = .002$, and $\sigma_A = .005$.

- makes the economy much riskier to agents
- increases volatility of stochastic discount factor

Best Fit

EZ Prefs

2.95

1.32

memo: quasi-CRRA		2	35
sd[x ⁽¹⁰⁾]	23.43	4.39	11.59
mean[$x^{(10)}$]	1.76	.005	.859
sd[<i>i</i> ⁽¹⁰⁾ - <i>i</i>]	1.33	0.64	1.15
mean[$i^{(10)} - i$]	1.43	018	.758
$sd[\psi^{(10)}]$	0.54	.000	.183
mean[$\psi^{(10)}$]	1.06	.005	.872
sd[<i>i</i> ⁽¹⁰⁾]	2.41	0.65	1.84
sd[<i>r</i>]	2.30	0.66	1.35
sd[<i>i</i>]	2.71	1.17	2.88
$sd[\pi]$	2.52	1.12	3.14
sd[<i>w</i> ′]	0.82	1.43	1.90

Table 3: Moments with Long-Run Productivity Risk

U.S. Data

1961-2007

1.19

1.71

Variable

sd[C]

sd[L]

EU

Preferences

0.92

1.03

Long-Run Risks ○○●○○○○

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Long-Run Inflation Risk

Introduce long-run inflation risk to make long-term bonds more risky:

- same idea as Bansal-Yaron (2004), but with nominal risk rather than real risk
- long-term inflation expectations more observable than long-term consumption growth
- other evidence (Kozicki-Tinsley, 2003, Gürkaynak, Sack, Swanson, 2005) that long-term inflation expectations in the U.S. vary

DSGE Model with EZ Preferences

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Long-Run Inflation Risk



DSGE Model with EZ Preferences

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Long-Run Inflation Risk

Suppose:

$$\pi_t^* = \rho_\pi^* \pi_{t-1}^* + \varepsilon_t^{\pi^*}$$

DSGE Model with EZ Preferences

Long-Run Risks ○○○○●○○ Conclusions

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Long-Run Inflation Risk

Suppose:

$$\pi_t^* = \rho_\pi^* \pi_{t-1}^* + \varepsilon_t^{\pi^*}$$

Then:

- inflation is volatile, but not risky
- in fact, long-term bonds act like insurance: when π^{*} ↑, then C ↑ and p⁽¹⁰⁾ ↓
- result: term premium is *negative*

DSGE Model with EZ Preferences

Long-Run Risks ○○○○○●○

Long-Run Inflation Risk

Consider instead:

$$\pi_t^* = \rho_{\pi}^* \pi_{t-1}^* + (1 - \rho_{\pi}^*) \theta_{\pi^*} (\overline{\pi}_t - \pi_t^*) + \varepsilon_t^{\pi^*}$$



Long-Run Risks ○○○○○●○

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Long-Run Inflation Risk

Consider instead:

$$\pi_t^* = \rho_\pi^* \pi_{t-1}^* + (1 - \rho_\pi^*) \theta_{\pi^*} (\overline{\pi}_t - \pi_t^*) + \varepsilon_t^{\pi^*}$$

- θ_{π^*} describes pass-through from current π to long-term π^*
- Gürkaynak, Sack, and Swanson (2005) found evidence for $\theta_{\pi^*} > 0$ in U.S. bond response to macro data releases
- makes long-term bonds act less like insurance: when technology/supply shock, then π ↑, C ↓, and p⁽¹⁰⁾ ↓ supply shocks become very costly
- The term premium is *positive*, closely associated with θ_{π*}

Table 4: Moments with Long-Run Inflation Risk

Variable	U.S. Data 1961-2007	EU Preferences	Best Fit EZ Prefs
sd[C]	1.19	1.92	1.86
sd[L]	1.71	3.33	1.73
sd[w ^r]	0.82	2.55	1.45
$sd[\pi]$	2.52	5.00	3.22
sd[<i>i</i>]	2.71	4.74	2.99
sd[<i>r</i>]	2.30	2.61	1.48
sd[<i>i</i> ⁽¹⁰⁾]	2.41	3.32	1.94
mean[$\psi^{(10)}$]	1.06	.002	.748
$sd[\psi^{(10)}]$	0.54	.001	.431
mean[<i>i</i> ⁽¹⁰⁾ – <i>i</i>]	1.43	062	.668
sd[<i>i</i> ⁽¹⁰⁾ - <i>i</i>]	1.33	1.60	1.11
mean[$x^{(10)}$]	1.76	.003	.737
sd[x ⁽¹⁰⁾]	23.43	16.96	11.83
memo: quasi-CRRA		2	65

Motivation 00000	DSGE Model with EZ Preferences	Long-Run Risks	Conclusions •
Conclusions	8		

 Epstein-Zin preferences appear to solve bond premium puzzle in DSGE model, as in an endowment economy: agents are risk-averse and cannot offset long-run real or nominal risks

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Motivation 00000	DSGE Model with EZ Preferences	Long-Run Risks	Conclusions •
Conclusions	3		

- Epstein-Zin preferences appear to solve bond premium puzzle in DSGE model, as in an endowment economy: agents are risk-averse and cannot offset long-run real or nominal risks
- 2 Long-run risks reduce the required quasi-CRRA, increase volatility of risk premia, help fit financial moments

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Motivation 00000	DSGE Model with EZ Preferences	Long-Run Risks	Conclusions
Conclusions	3		

- Epstein-Zin preferences appear to solve bond premium puzzle in DSGE model, as in an endowment economy: agents are risk-averse and cannot offset long-run real or nominal risks
- 2 Long-run risks reduce the required quasi-CRRA, increase volatility of risk premia, help fit financial moments
- Unresolved issues:
 - Reliance on technology shocks, not π^* shocks
 - Fitting more moments, estimation from data
 - Is quasi-CRRA appropriate measure of risk aversion?

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Little feedback from asset prices to economy