

# Booms and Systemic Banking Crises

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- Better understand the joint dynamics of regular business cycles and systemic banking crises (SBCs)
- Account for the few features common to SBCs (Reinhart and Rogoff, 2009; Jordà et al., 2011; Claessens et al., 2011; Schularick and Taylor, 2012):
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  - Key Fact #3: SBCs are "**credit booms gone wrong**"

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- From a policy perspective, our framework is a step forward towards:
  - DSGE-based crisis prevention policy analysis
  - **DSGE-based early warning signals**

- Stylized facts
- Comparison with the literature
- RBC model with systemic banking crises
- Quantitative analysis
- Concluding remarks

# Stylized facts

SBCs are rare and bring about deep and long recessions

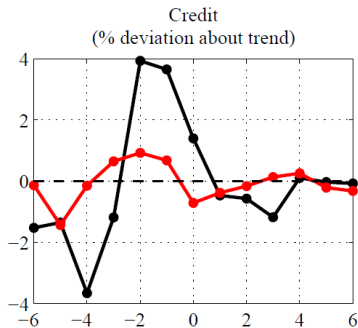
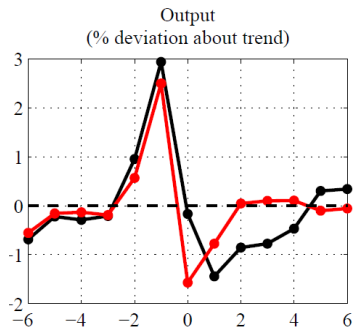
## Frequency, magnitude, and duration of systemic banking crises

	Frequency (%)	Magnitude (%) from peak to trough	Duration (Years)
All banking crises	4.49	–	–
Systemic Banking Crises (SBC)	<b>2.42</b>	–	–
All recessions	10.20	4.86 (5.91)	1.85
Recessions with SBC (A)	23.86	<b>6.74</b> (6.61)	<b>2.59</b>
Recessions w/o SBC (B)	76.13	<b>4.27</b> (5.61)	<b>1.61</b>
Test $A \neq B$ , p-value (%)	–	2.61	0.00

Source: Schularik et al. (2011), data for 14 OECD countries, 1870-2008  
Crises defined as in Laeven and Valencia (2008)

# Stylized facts

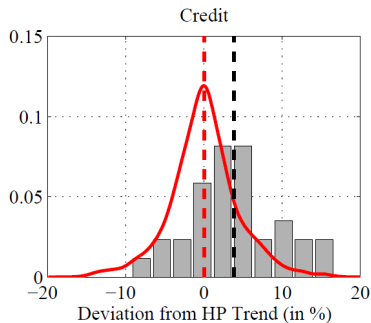
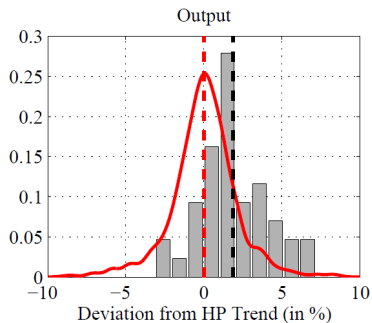
SBCs follow credit booms



—●— Recessions with a Financial Crisis, —●— Other Recessions

# Stylized facts

SBCs are not random





- Textbook stochastic optimal growth model (RBC)
- Heterogenous banks endowed with intermediation and storage technologies
- Interbank market subject to MH and AI
- A Systemic Banking Crisis is an inter-bank market freeze
- Spill-over effects between the interbank market, the retail corporate loan market, and the real economy

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- 3 **Financial recessions follow credit booms. They are deeper and last longer because they come with a credit crunch**

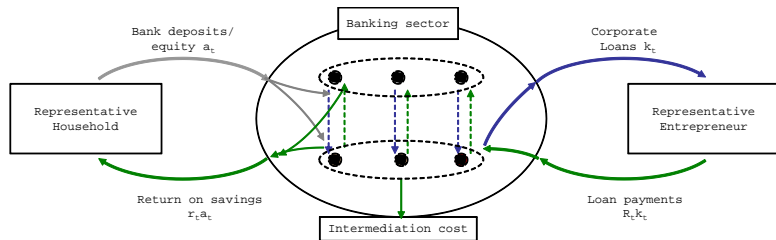
# Main Results

- 1 Model features a (small) financial accelerator in normal times; calibrated to generate financial crises every 40 years
- 2 The **typical banking crisis follows upon an unusually long sequence of small, positive, transitory productivity shocks** — Not a large negative financial shock
- 3 Financial recessions follow credit booms. They are deeper and last longer because they come with a credit crunch
- 4 The likelihood, depth, and length of a financial recession increase with the intensity of the credit boom that precedes it

- Gertler-Kiyotaki (2009), Gertler-Karadi (2010):
  - ≠ Full equilibrium non-linearities, such as sudden bank runs
- Bianchi (2009), Bianchi-Mendoza (2010):
  - ≠ Endogenous interest rates play a key role
- Brunnermeier-Sannikov (2012), He-Krishnamurthy (2012):
  - ≠ Typical crisis follows a rare, long sequence of positive TFP shocks
  - ≠ Typical crisis identified as a bank run, not as a binding borrowing constraint
- Gertler-Kiyotaki (2012)
  - ≠ Bank run is market based and rationally expected

# Model setup

## Overview



- Financial flows at the end of period  $t-1$  ("core activity")
- Financial flows at the beginning of period  $t$  ("core activity")
- ← Financial flows at the end of period  $t$  ("core activity")
- Financial flows at the beginning of period  $t$  ("non-core activity")
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- ● ● Banks are heterogeneous w.r.t. their financial intermediation costs

# Representative Household and Firm

- Firm:  $\max_{\{k_t, h_t\}} \pi_t = F(k_t, h_t; z_t) + (1 - \delta)k_t - R_t k_t - w_t h_t$
- Household:

$$\max_{\{a_{t+\tau+1}, c_{t+\tau}, h_{t+\tau}\}_{\tau=0}^{\infty}} \mathbb{E}_t \sum_{\tau=0}^{\infty} \beta^{\tau} u(c_{t+\tau}, h_{t+\tau})$$

subject to budget constraint

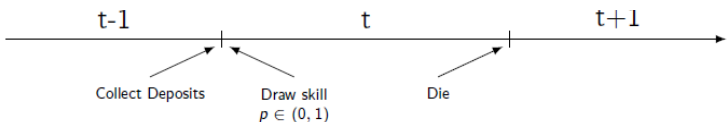
$$c_t + a_{t+1} = r_t a_t + w_t h_t + \pi_t$$

- Notice that  $r_t \leq R_t$  (spread) and  $k_t \leq a_t$  (credit crunch)



# The Banking Sector

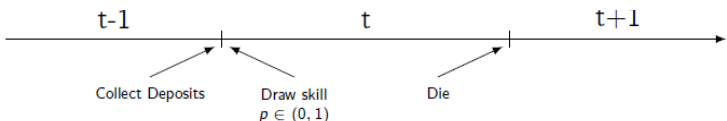
- Banks are atomistic, competitive, and price takers
- Heterogeneous 1-period banks



- Bank  $p$ 's net return per unit of corporate loan is  $pR_t$
- Beneficial to relocate funds: unskilled banks lend to skillful banks on an interbank market. But relocation impaired due to:

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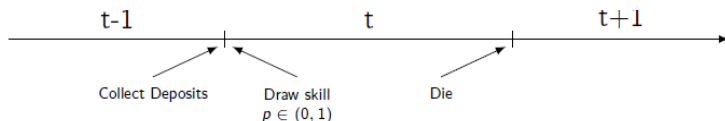
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- Beneficial to relocate funds: unskilled banks lend to skillful banks on an interbank market. But relocation impaired due to:
  - **Asymmetric information:**  $p$  is private information
  - **Moral hazard:** bank  $p$  may borrow  $\phi_t$  and run away

- Bank  $p$  has 4 options:
  1. Lend to other banks on the market  $\implies \rho_t$
  2. Store goods  $\implies \gamma$
  3. Raise funds  $\phi_t$  from market and lend to firm  $\implies pR_t(1 + \phi_t)$
  4. Raise funds  $\phi_t$  from market and walk away  $\implies \gamma(1 + \theta\phi_t)$
- Notice that the incentive to divert depends on corporate loan  $R_t$ 
  - The higher  $R_t$ , the lower the incentive to divert

# The Borrowing Bank's Problem

- Borrowing bank  $p$  solves:

$$\max_{\phi_t} r_t(p) \equiv pR_t(1 + \phi_t) - \rho_t\phi_t$$

$$PC: \quad pR_t(1 + \phi_t) - \rho_t\phi_t \geq \rho_t \quad \Rightarrow \quad p \geq \bar{p}_t \equiv \frac{\rho_t}{R_t}$$

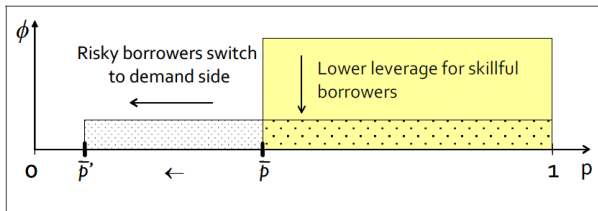
$$IC: \quad \gamma(1 + \theta\phi_t) \leq \rho_t \quad \Rightarrow \quad \phi_t = (\rho_t - \gamma)/\theta\gamma$$

- Profits are fully distributed to household:  $r_t \equiv \int_0^1 r_t(p) d\mu(p)$

# Interbank Market Equilibrium

Interbank market clearing condition

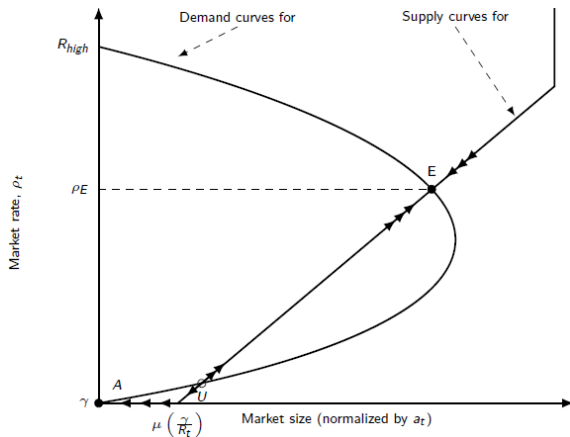
$$\underbrace{\mu(\bar{\rho}_t)}_{\text{Supply (+)}} = \underbrace{\underbrace{(1 - \mu(\bar{\rho}_t))}_{\text{"extensive margin" (-)} \times \underbrace{\phi_t}_{\text{"intensive margin" (+)}}}_{\text{Demand bends backward (+ or -)}}$$



Two opposite effects on aggregate demand of a decrease in  $\rho_t$

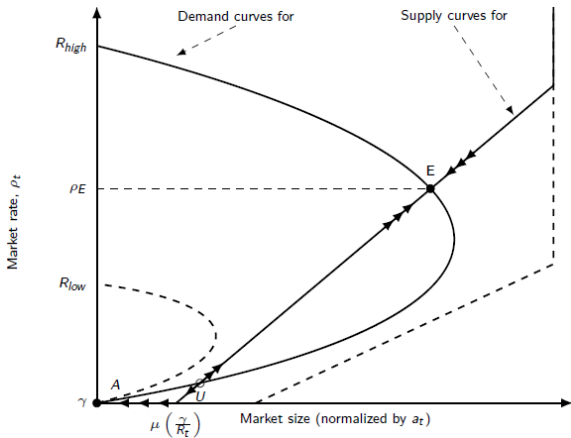
# Interbank Market Equilibrium

Trade takes place when the corporate loan rate is high



# Interbank Market Equilibrium

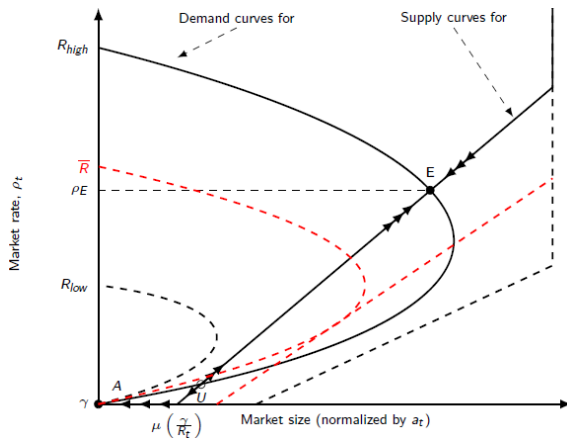
Trade is impossible when the corporate loan rate is low





# Interbank Market Equilibrium

Corporate loan rate threshold



# The Banking Sector

## Return on equity and corporate loan supply

- Return on equity:

$$r_t = \begin{cases} R_t \int_{\bar{p}_t}^1 p \frac{d\mu(p)}{1-\mu(\bar{p}_t)} , & \text{if an equilibrium with trade exists} \\ R_t \left( \frac{\gamma}{R_t} \mu \left( \frac{\gamma}{R_t} \right) + \int_{\frac{\gamma}{R_t}}^1 p d\mu(p) \right) , & \text{otherwise.} \end{cases}$$

- Corporate loan supply

$$k_t^s = \begin{cases} a_t , & \text{if an equilibrium with trade exists} \\ \left( 1 - \mu \left( \frac{\gamma}{R_t} \right) \right) a_t , & \text{otherwise} \end{cases}$$

- **Proposition 2 (Interbank loan market freeze):** *The interbank loan market is at work if and only if  $a_t \leq \bar{a}_t \equiv f_k^{-1}(\bar{R} + \delta - 1; z_t)$ , and freezes otherwise.*
- **Proposition 3 (Credit crunch):** *An interbank market freeze is accompanied with a sudden fall in the supply of corporate loans  $k_t^S$  (i.e. given  $z_t$ ,  $\lim_{a_t \searrow \bar{a}_t} k_t^S < \lim_{a_t \nearrow \bar{a}_t} k_t^S$ ), as well as by a sudden increase in the interest rate spread  $R_t/r_t$  (i.e. given  $z_t$ ,  $\lim_{a_t \searrow \bar{a}_t} R_t/r_t > \lim_{a_t \nearrow \bar{a}_t} R_t/r_t$ ).*

# The Banking Sector

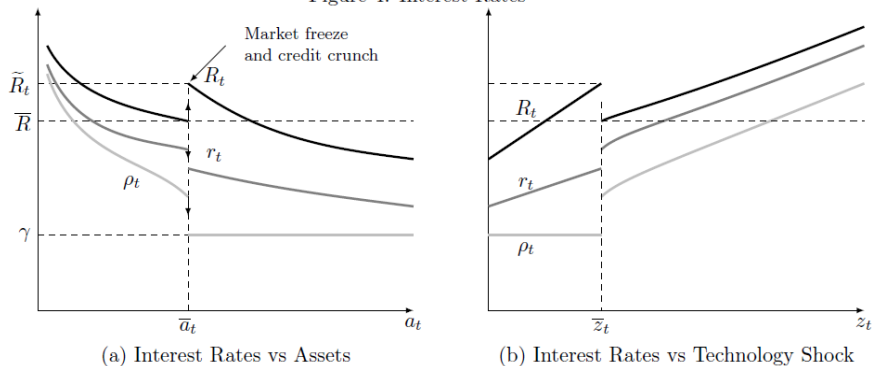
## Absorption capacity and financial imbalances

- Interbank market improves efficiency but freezes when  $R_t < \bar{R}$
- In general equilibrium,  $R_t$  is driven by savings ( $a_t$ ) and technology ( $z_t$ ). Hence the interbank market freezes when  $a_t > \bar{a}(z_t)$
- **Threshold  $\bar{a}(z_t)$  is the banking sector's "absorption capacity"**
- A measure of financial imbalances is  $\bar{a}_t(z_t) - a_t$

# The Banking Sector

## Interest rates

Figure 4: Interest Rates



# The Banking Sector

## Core and non-core liabilities

### Bank balance sheets

<i>Normal times</i>				<i>Crisis times</i>			
A	L	A	L	A	L	A	L
$(1 + \phi_t) a_t$	$a_t$	$a_t$	$a_t$	$a_t$	$a_t$	$a_t$	$a_t$
	$\phi_t a_t$	$a_t$				$a_t$	
$p \geq \bar{p}_t$		$p < \bar{p}_t$		$p \geq \frac{\gamma}{R_t}$		$p < \frac{\gamma}{R_t}$	

Size is  $a_t + (1 - \mu(\bar{p}_t)) \phi_t a_t$

Size is  $a_t$

# The Banking Sector

Two-way relationship between the retail and the wholesale loan markets

- Whether the interbank market is functioning depends on the corporate loan market equilibrium rate  $R_t^*$
- $R_t^*$  depends on whether the interbank market is functioning
- The model must be solved taking these interactions into account:
  - 1 Conjecture the interbank market operates and solve for  $R_t^*$
  - 2 Verify whether indeed the interbank market operates ( $R_t^* \geq \bar{R}$ )
  - 3 In the negative, solve for  $R_t^*$  under a credit crunch

- Production function:  $F(k_t, h_t; z_t) \equiv z_t k_t^\alpha h_t^{1-\alpha}$  with  $\alpha \in (0, 1)$
- Utility function:  $u(c_t, h_t) = \frac{1}{1-\sigma} \left( c_t - \vartheta \frac{h_t^{1+v}}{1+v} \right)^{1-\sigma}$
- Cdf of bank skills:  $\mu(p) = p^\lambda$
- Real economy: standard calibration on US (annual) post-WWII data
- Financial sector  $(\gamma, \theta, \lambda)$  is calibrated so that:
  - Crisis probability is 2.5%
  - Average interest rate spread is 1.71%
  - Average corporate loan rate of 4.35%



### Parameters of the model

Discount factor	$\beta$	1/1.03
Risk aversion	$\sigma$	4.500
Frisch elasticity	$v$	1/3
Labor disutility	$\vartheta$	0.944
Capital elasticity	$\alpha$	0.300
Capital depreciation rate	$\delta$	0.100
Standard dev. productivity shock	$\sigma_z$	0.018
Persistence of productivity shock	$\rho_z$	0.900
Bank distribution; $\mu(p) = p^\lambda$	$\lambda$	24
Diversion cost	$\theta$	0.1
Storage technology	$\gamma$	0.936

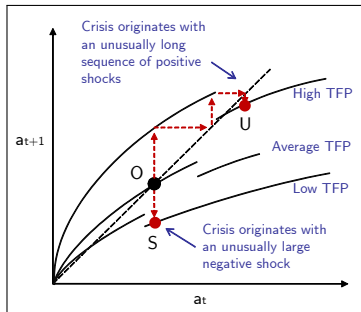
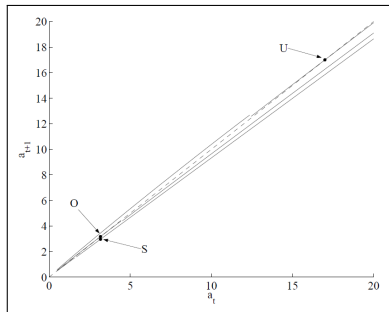
# Quantitative Analysis

## Solution method

- The model is solved numerically by a collocation method
- Discretize the TFP level (Tauchen and Hussey, 1991)
- Decision rule for  $a_{t+1}$  is approximated by a function of Chebychev polynomials
- The optimal decision rule is obtained as the fixed point solution to the Euler equation

# Quantitative Analysis

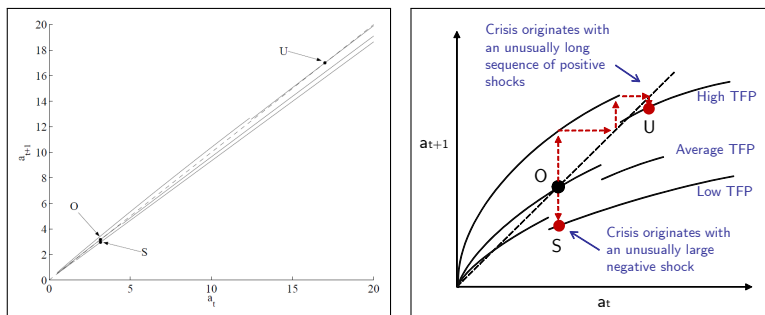
Optimal savings rule: exogenous versus endogenous crises



- Variety of crises: shock-driven (S) and credit boom-driven (U)

# Quantitative Analysis

Optimal savings rule: exogenous versus endogenous crises



- Variety of crises: shock-driven (S) and credit boom-driven (U)
- History suggests that credit-boom driven crises prevail

# Quantitative Analysis

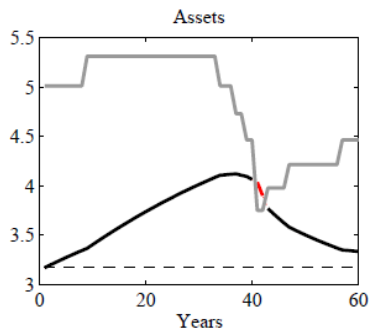
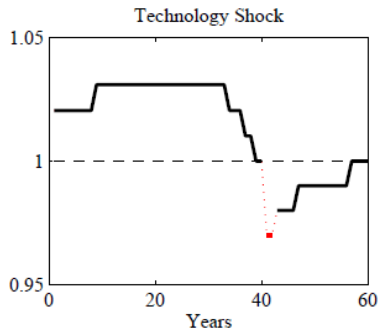
## Intuition behind endogenous SBCs

- 1 At the beginning, a positive shock brings TFP above its mean
  - Credit demand rises. Return on savings goes up. The household accumulates assets for *consumption smoothing*
  - The **credit boom is initially demand-driven**
- 2 TFP goes down back to mean but remains above it for a long time
  - Credit demand decreases, while the household keeps on accumulating savings
  - The **credit boom becomes supply-driven**
- 3 The household accumulates assets for *precautionary motives*, which works to reduce interest rates and to raise further the likelihood of a crisis
- 4 A SBC breaks out as the corporate loan rate crosses its threshold

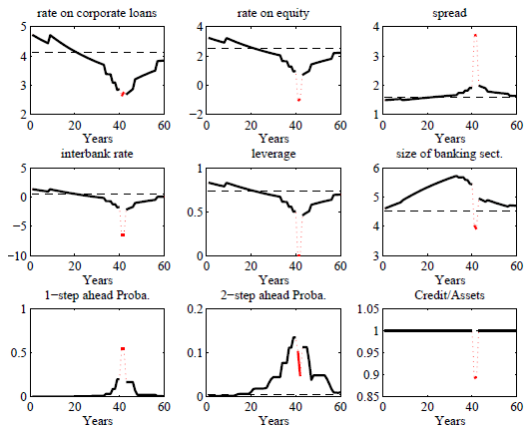
# Quantitative Analysis

## Typical path to crisis

### Typical path



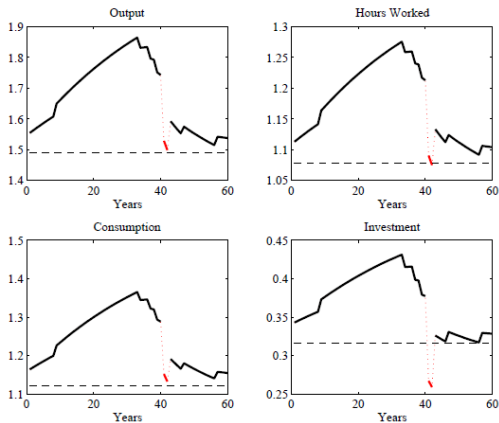
### Financial variables dynamics along typical path



# Quantitative Analysis

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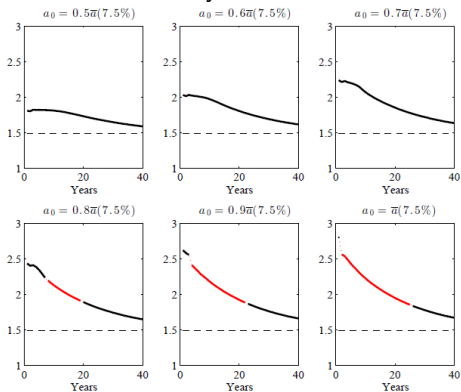
### Real variables dynamics along typical path





### Sensitivity of output dynamics to initial conditions

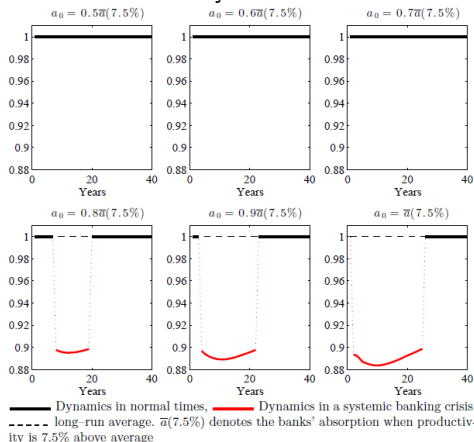
TFP is initially 7.5% above mean



— Dynamics in normal times, — Dynamics in a systemic banking crisis,  
- - - long-run average.  $\bar{\alpha}(7.5\%)$  denotes the banks' absorption when productivity is 7.5% above average

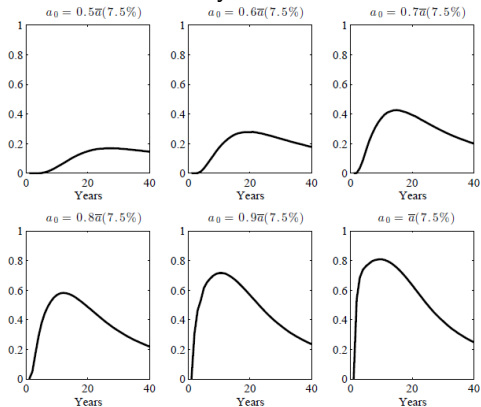
### Sensitivity of credit dynamics to initial conditions

TFP is initially 7.5% above mean



### Sensitivity of the frequency of SBCs to initial conditions

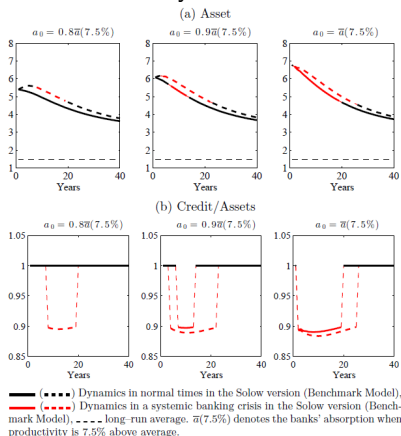
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This figure reports the evolution of the frequency of SBCs during the transition toward the average steady state.

### Sensitivity of the frequency of SBCs to initial conditions

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# Quantitative Assessment

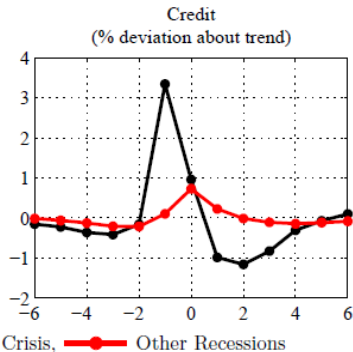
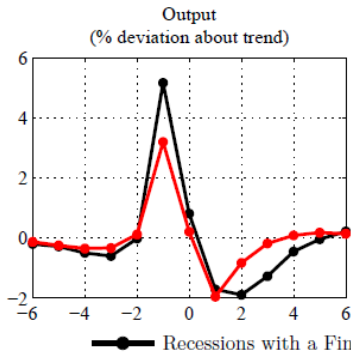
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## Frequency, magnitude, and duration of systemic banking crises

	Frequency (%)	Magnitude (%) from peak to trough	Duration (Years)
Systemic Banking Crises (SBC)	<b>2.69</b>	–	–
All recessions	10.00	12.08 (7.30)	2.08
Recessions with SBC (A)	13.00	<b>17.87</b> (10.50)	<b>2.62</b>
Recessions w/o SBC (B)	87.00	<b>10.04</b> (6.73)	<b>1.90</b>

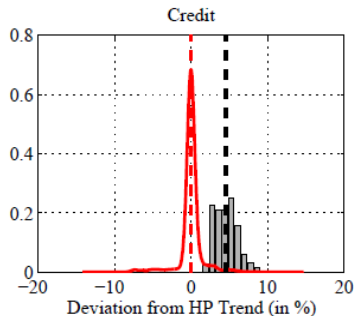
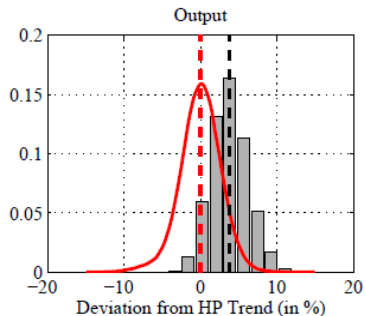
# Quantitative Assessment

SBCs follow credit booms

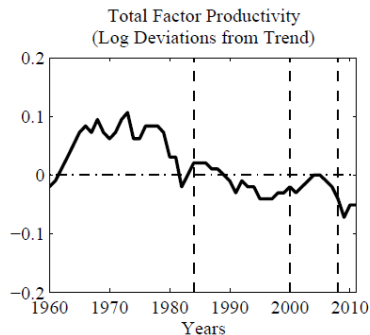
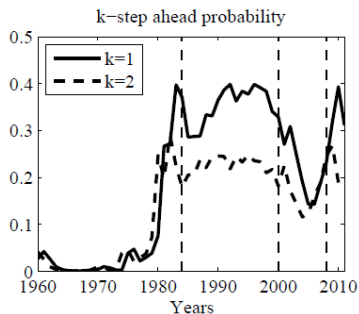


# Quantitative Assessment

SBCs are not random



### Crisis probabilities for the US



Note: The vertical thin dashed lines correspond to the 1984 Savings & Loans, the 2000 dotcom and 2008 crises.



## Changes in standard parameters

	Benchmark	$\sigma$	$\theta$	$\lambda$	$\sigma_z$	$\rho_z$
		10	0.20	35	0.02	0.95
interbank rate ( $\rho$ )	0.86	0.23	0.40	1.34	0.89	0.72
Corporate rate ( $R$ )	4.35	3.70	5.50	3.70	4.32	4.29
Return on deposit/equity ( $r$ )	2.64	1.61	2.61	2.67	2.55	2.59
Spread ( $R - r$ )	1.71	2.09	2.89	1.03	1.77	1.70
$\bar{R}$	2.43	2.43	4.83	0.41	2.43	2.43
Probability of a crisis	2.69	5.43	7.34	0.16	3.35	1.90
Average duration	2.62	4.08	5.06	1.87	2.82	2.92
Average amplitude	17.87	19.00	16.90	15.80	19.36	16.08

# Bank Leverage, Bank Defaults

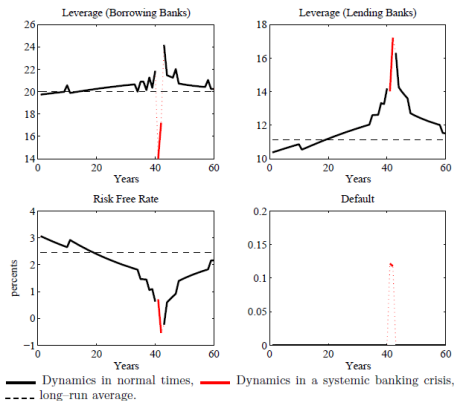
- Absent frictions between banks and household, bank leverage is undeterminate and bank default is not defined
- Two more assumptions to pin down leverage:
  - Bank deposits are safe assets (non state contingent return)
  - Bank managers are risk neutral (unlike household)
- One more assumption to introduce defaults:
  - Household (bank shareholder) has partial liability

# Bank Leverage, Bank Defaults

Typical path to crisis

## Leverage and bank default dynamics along typical path

Figure 19: Typical Path: Leverage and Default



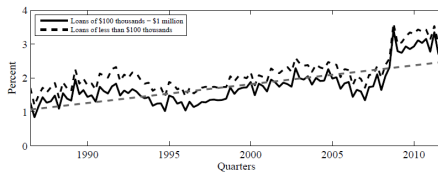
# Concluding Remarks

- Develop a simple DSGE model with SBCs
- SBCs are not caused by large, negative, financial shocks but rather by long sequences of small, positive, productivity shocks
- Highlight the role of financial imbalances, consumption smoothing, and precautionary savings
- From a policy making perspective:
  - Framework for both crisis management and crisis prevention
  - DSGE-based probability of a crisis

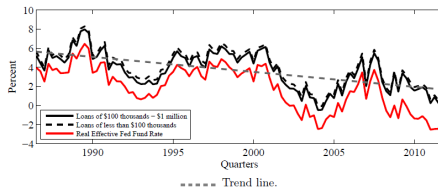


Figure C.4: Evolution of Various Corporate Loan Spreads

(a) Spread: Corporate loan rates - Federal Fund Rate



(b) Underlying Real Corporate Loan Rates



# The Model in a Nutshell

$$\begin{aligned}
 y_t &= z_t k_t^\alpha h_t^{1-\alpha} + (\gamma + \delta - 1) (a_t - k_t) \\
 R_t &= \alpha k_t^{\frac{-v(1-\alpha)}{v+\alpha}} z_t^{\frac{1+v}{v+\alpha}} \left( \frac{1-\alpha}{\vartheta} \right)^{\frac{1-\alpha}{v+\alpha}} + 1 - \delta \\
 \left( c_t - \vartheta \frac{h_t^{1+v}}{1+v} \right)^{-\sigma} &= \beta \mathbb{E}_t \left[ \left( c_{t+1} - \vartheta \frac{h_{t+1}^{1+v}}{1+v} \right)^{-\sigma} r_{t+1} \right] \\
 h_t &= \left( \frac{(1-\alpha)z_t}{\vartheta} \right)^{\frac{1}{v+\alpha}} k_t^{\frac{\alpha}{v+\alpha}} \\
 \bar{a}_t &\equiv \left( (1-\alpha)/\vartheta \right)^{\frac{1}{v}} \left( \alpha / (\bar{R} + \delta - 1) \right)^{\frac{v+\alpha}{v(1-\alpha)}} z_t^{\frac{1+v}{v(1-\alpha)}} \\
 i_t &= a_{t+1} - (1-\delta) a_t
 \end{aligned}$$

*Normal times*

$$\begin{aligned}
 k_t &= a_t \\
 \frac{r_t}{R_t} &= \int_{\bar{p}_t}^1 p \frac{d\mu(p)}{1-\mu(\bar{p}_t)} \\
 \bar{p}_t &= \frac{\rho_t}{R_t} \\
 R_t &= \frac{\rho_t}{\mu^{-1}\left(\frac{\rho_t - \gamma}{\rho_t - (1-\theta)\gamma}\right)} \\
 y_t &= c_t + i_t + (R_t - r_t) a_t
 \end{aligned}$$

*Crisis times*

$$\begin{aligned}
 k_t &= a_t - \mu(\gamma/R_t) a_t \\
 \frac{r_t}{R_t} &= \frac{\gamma}{R_t} \mu(\gamma/R_t) + \int_{\gamma/R_t}^1 p d\mu(p) \\
 \bar{p}_t &= \gamma/R_t \\
 \rho_t &= \gamma \\
 y_t &= c_t + i_t + (R_t - r_t) a_t - (R_t - \gamma) (a_t - k_t)
 \end{aligned}$$

# The Banking Sector

A reduced form

- Interest rate spread:

$$R_t - r_t = \begin{cases} \Delta_t^n & \text{if } a_t \leq \bar{a}_t(z_t) \\ \Delta_t^c & \text{otherwise} \end{cases}, \text{ with } \Delta_t^c > \Delta_t^n > 0$$

- Credit crunch:

$$a_t - k_t = \begin{cases} \psi_t^n = 0 & \text{if } a_t \leq \bar{a}_t(z_t) \\ \psi_t^c > 0 & \text{otherwise} \end{cases}$$

- Notice that all this is micro-founded