

# Financial Factors in Economic Fluctuations

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# Background

- Much progress made on constructing and estimating models that fit quarterly data well (Smets-Wouters, others).
- In practice the models abstract from details of financial markets and interaction with real economy.
- A common presumption: asset markets passively reflect fluctuations in standard shocks and contribute little to propagation.

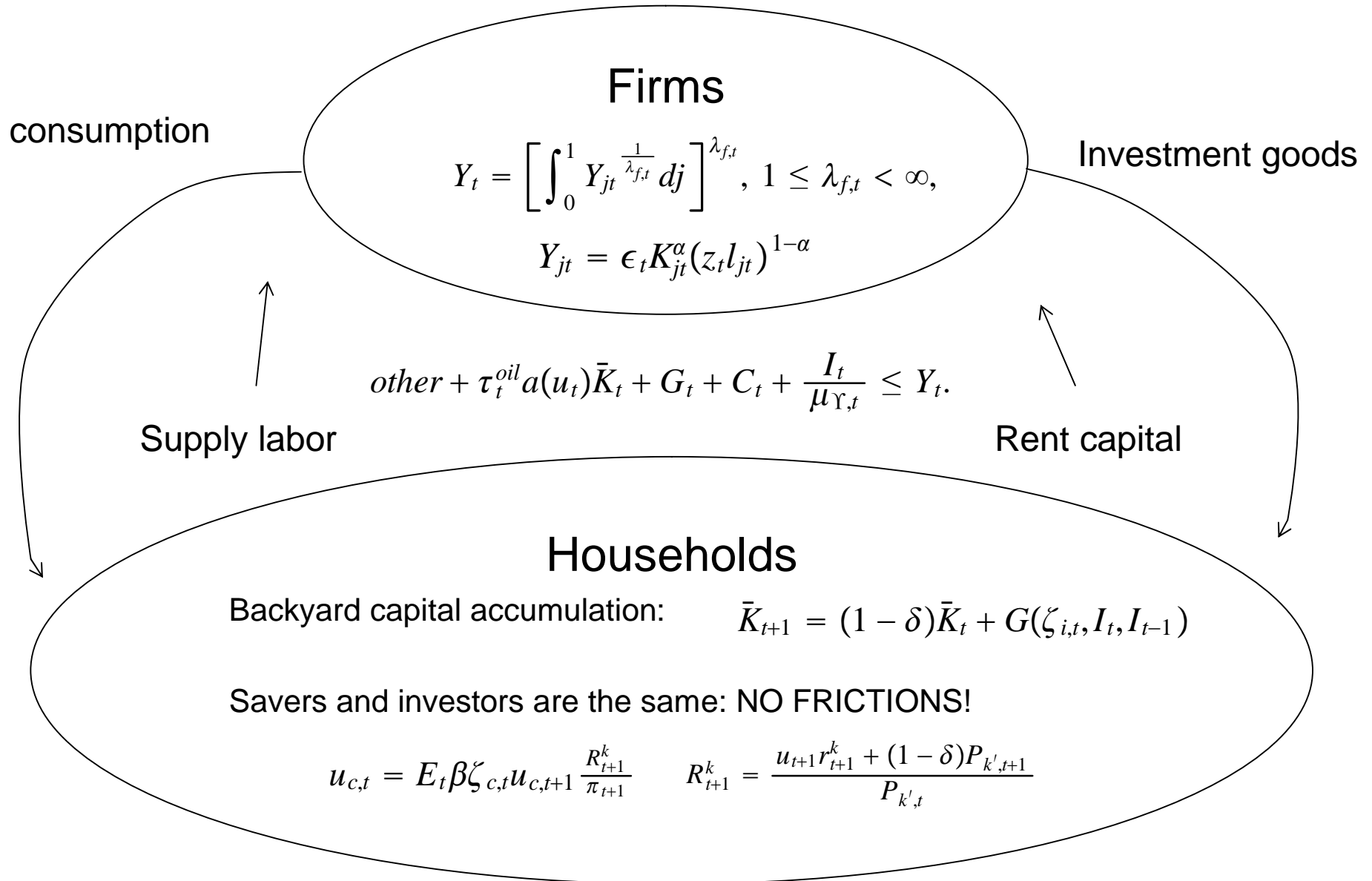
# What we do

- Integrate financial frictions into a standard DSGE model and estimate the model using EA and US data.
- Finding: integration of financial frictions changes inference about the shocks and propagation mechanisms governing economic fluctuations.
  - Identify a new shock, a ‘risk’ shock
  - Identify a new propagation mechanism.

# Outline

- Sketch the basic ingredients of the model.
- Present 5 results that motivate our conclusion

# Standard Model



# Extension to Incorporate Financial Frictions

- General idea:
  - Borrowing for two purposes:
    - Short term financing of working capital
    - Longer-term financing of capital.
  - Bank financing:
    - Issue assets that provide various degrees of transactions services to finance short term bank assets
    - Issue 'time deposits' to finance longer-term loans.

# Banks

- Financial system assets and liabilities:

Short-term Assets	Short-term Liabilities
- <i>Reserves</i>	- <i>Household demand deposits</i>
$A_t$	$D_t^h = A_t$
- <i>Short-term Working Capital Loans</i>	- <i>Firm demand deposits</i>
$S_t^w$	$D_t^f = S_t^w$
<b>"Long-term" loans (to entrepreneurs)</b>	<b>"Long-term" Liabilities (to households)</b>
$B_t$	$T_{t-1}$
	$D_t^m$

- Technology for producing transactions services:

$$\frac{D_t^h + D_t^f + \zeta D_t^m}{P_t} = a_t \left( (K_t^b)^\alpha (z_t l_t^b)^{1-\alpha} \right)^{\xi_t} \left( \frac{E_t^r}{P_t} \right)^{1-\xi_t}$$

# Households

- Preferences:

$$E_t^j \sum_{l=0}^{\infty} \beta^l \zeta_{c,t+l} \left\{ u(C_{t+l} - bC_{t+l-1}) - \psi_L \frac{h_{j,t+l}^{1+\sigma_L}}{1+\sigma_L} - v \frac{\left[ \left( \frac{(1+\tau^c)P_{t+l}C_{t+l}}{M_{t+l}} \right)^{(1-\chi_{t+l})\theta} \left( \frac{(1+\tau^c)P_{t+l}C_{t+l}}{D_{t+l}^h} \right)^{(1-\chi_{t+l})(1-\theta)} \left( \frac{(1+\tau^c)P_{t+l}C_{t+l}}{D_{t+l}^m b} \right)^{\chi_{t+l}} \right]^{1-\sigma_q}}{1-\sigma_q} \right\},$$

- Features:

- Habit formation in consumption, differentiated Labor
- Monopolistic supplier of specialized labor input (EHL)
- Enjoy deposits services of two bank assets
- Hold time deposits



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- Features:

- Habit formation in consumption, differentiated Labor
- Monopolistic supplier of specialized labor input (EHL)
- Enjoy deposits services of two bank assets
- Hold time deposits
- Access to 10-year bond, with gross return

exogenous shock designed to capture any failure of the model to match  $R_t^{long}$

compared with data on 10 year bond returns

$\overbrace{\sigma_t}^{long}$

$(1 + \overbrace{R_t}^{long})$

# Monetary Policy

- Monetary policy rule:

$$\begin{aligned}\hat{R}_t^e &= \rho_i \hat{R}_{t-1}^e + (1 - \rho_i) \alpha_\pi \frac{\pi}{R^e} [E_t(\hat{\pi}_{t+1}) - \hat{\pi}_t^{target}] \\ &+ (1 - \rho_i) \frac{\alpha_y}{4R^e} \log\left(\frac{GDP_t}{\mu_z^* GDP_{t-1}}\right) + (1 - \rho_i) \alpha_{d\pi} \frac{\pi}{R^e} (\hat{\pi}_t - \hat{\pi}_{t-1}) \\ &+ (1 - \rho_i) \frac{\alpha_b}{4R^e} \log\left(\frac{B_{t+1}}{\mu_z^* B_t}\right) \frac{1}{400R^e} \varepsilon_t,\end{aligned}$$

- Monetary policy shock:

$$\varepsilon_t \sim \text{white noise}$$

- Inflation target:

$$\hat{\pi}_t^{target} = \rho_\pi \hat{\pi}_{t-1}^{target} + \varepsilon_t^{target}, \quad E(\varepsilon_t^{target})^2 = \sigma_\pi,$$

$$\rho_\pi = 0.965, \quad \sigma_\pi = 0.00035$$

# Entrepreneurs (BGG)

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- Own and Rent the Stock of Capital

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- Own and Rent the Stock of Capital
- Period  $t$  :
  - Go to bank with own net worth and obtain loan
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  - Experience an idiosyncratic productivity shock:  $\omega \bar{K}_{t+1}$ ,  $\omega \sim F(\omega; \sigma_t)$

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- Period  $t + 1$  :
  - Choose capital utilization rate and rent out capital services:  $u_{t+1} \omega \bar{K}_{t+1}$
  - Cost of utilization:  $\tau_{t+1}^{oil} a(u_{t+1}) \Upsilon^{-(t+1)} \omega \bar{K}_{t+1}$

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$$V_{t+1} = \text{real earnings on capital (rent plus capital gains)}_t$$
$$- \frac{\text{nominal rate of interest}_{t-1}}{\pi_t} \text{real debt to banks}_{t-1}$$

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Source of Fisher deflation effect



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$$\text{Net Worth}_{t+1} = \gamma(V_{t+1} + W_{t+1}^e) + (1 - \gamma)W_{t+1}^e$$

# Prediction of financial friction model:

- Shocks that drive output and price in the same direction ('demand') accelerated by financial frictions.
  - Fisher and earnings effects reinforce each other.
- Shocks that drive output and price in opposite directions ('supply') not much affected by financial frictions.
  - Fisher and earnings effects cancel each other.

# Risk Shock and News

- Assume

iid, univariate innovation to  $\hat{\sigma}_t$

$$\hat{\sigma}_t = \rho_1 \hat{\sigma}_{t-1} + \underbrace{u_t}$$

- Agents have advance information about pieces of  $u_t$

$$u_t = \xi_t^0 + \xi_{t-1}^1 + \dots + \xi_{t-8}^8$$

$$\xi_{t-i}^i \sim \text{iid}, E(\xi_{t-i}^i)^2 = \sigma_i^2$$

$$\xi_{t-i}^i \sim \text{piece of } u_t \text{ observed at time } t - i$$

# Estimation

- EA and US data covering 1985Q1-2007Q2

$$X_t = \begin{pmatrix} \Delta \log\left(\frac{N_{t+1}}{P_t}\right) \\ \pi_t \\ \log(\text{per capita hours}_t) \\ \Delta \log\left(\frac{\text{per capita credit}_t}{P_t}\right) \\ \Delta \log(\text{per capita GDP}_t) \\ \Delta \log\left(\frac{W_t}{P_t}\right) \\ \Delta \log(\text{per capita } I_t) \\ \Delta \log\left(\frac{\text{per capita } M1_t}{P_t}\right) \\ \Delta \log\left(\frac{\text{per capita } M3_t}{P_t}\right) \\ \Delta \log(\text{per capita consumption}_t) \\ \text{External Finance Premium}_t \\ R_t^{long} - R_t^e \\ R_t^e \\ \Delta \log P_{I,t} \\ \Delta \log \text{real oil price}_t \\ \Delta \log\left(\frac{\text{per capita Bank Reserves}_t}{P_t}\right) \end{pmatrix},$$

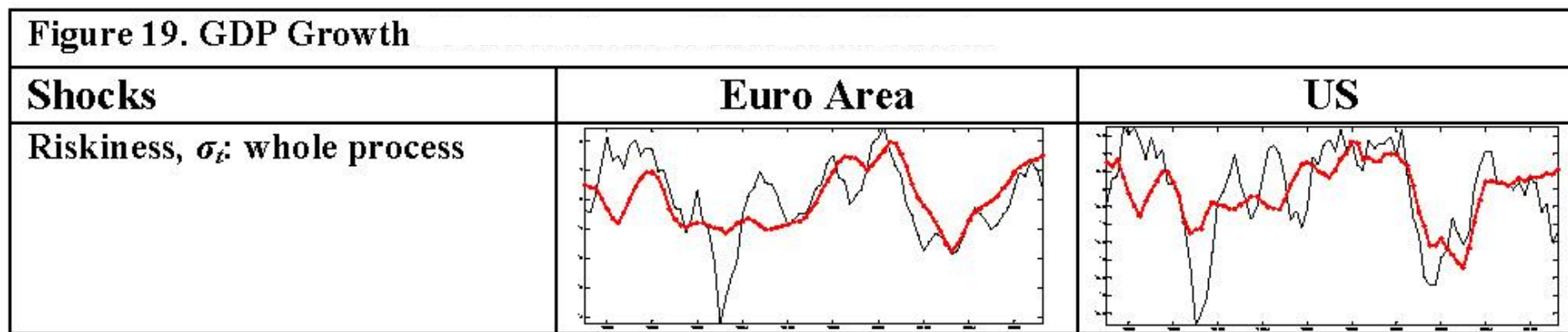
- Standard Bayesian methods (e.g., SW)
- We remove sample means from data and set steady state of  $X$  to zero in estimation.

# Summary of results

- Risk shocks are an important source of fluctuations.
- News on the risk shocks is important.
- The Fisher debt-deflation channel has a substantial impact on propagation.
- Shocks to money demand and mechanism of producing inside money relatively unimportant.
- Out-of-Sample RMSEs of the model achieve the high standards set by SW.

# Risk Shocks are Important

Actual data versus what actual data would have been if there were only risk Shocks:



Note:

- (1) as suggested by the picture, risk shocks are relatively important at the lower frequencies
- (2) We find that they are the single most important source of low frequency fluctuation in the EA, and a close second (after permanent tech shocks) in the US



Table: Variance Decomposition, HP filtered data, EA

shock	$x$							
	output	consumption	investment	hours	inflation	labor productivity	interest rate	
$\sigma_\gamma$	0.43	0.06	0.92	0.80	0.24	1.52	0.30	
$\sigma_\sigma$	2.88	0.19	5.11	6.57	0.88	13.17	1.08	
$\sigma_{\sigma^{\text{signal}}}$	20.09	1.81	38.09	15.96	9.22	38.24	9.80	
$\sigma_\sigma$ and $\sigma_{\sigma^{\text{signal}}}$	22.96	2.00	43.20	22.53	10.09	51.41	10.88	
all shocks	100.00	100.00	100.00	100.00	100.00	100.00	100.00	100.00

It's the signals!

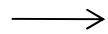




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$\sigma_{\xi_i}$	24.57	1.72	51.14	30.69	10.17	5.22	11.56	
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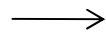




Table: Variance Decomposition, HP filtered data, EA

	$x$							
	shock	stock market	credit	spread	term structure	real M1	real M3	
Markup	$\sigma_{\lambda_f}$	—————→				12.36		
Banking tech	$\sigma_{x^b}$				0.10			
Capital tech	$\sigma_{\mu_Y}$				0.07			
Money demand	$\sigma_{\chi}$				0.00			
Government	$\sigma_g$				0.07			
Permanent tech	$\sigma_{\mu_z^*}$				0.14			
Gamma shock	$\sigma_{\gamma}$				0.33			
Temporary tech	$\sigma_{\epsilon}$				3.40			
Monetary policy	$\sigma_{\epsilon^{\text{policy}}}$	—————→				25.76		
Risk, contemp	$\sigma_{\sigma}$				0.97			
Signals on risk	$\sigma_{\sigma^{\text{signal}}}$				6.79			
Risk and signals	$\sigma_{\sigma}$ and $\sigma_{\sigma^{\text{signal}}}$	—————→				7.76		
Discount rate	$\sigma_{\xi_c}$				3.99			
Marginal eff of I	$\sigma_{\xi_i}$	—————→				8.77		
Price of oil	$\sigma_{\tau^{\text{oil}}}$				0.56			
Error in long rate	$\sigma_{\text{long}}$	—————→				36.05		
	measurement error				0.32			
	inflation target				0.34			
	all shocks				100.00			

Table: Variance Decomposition, HP filtered data, EA

		$x$					
shock		stock market	credit	spread	term structure	real M1	real M3
<b>Gamma shock</b>	$\sigma_\gamma$	5.37	25.82	1.86	0.33	0.13	0.15
<b>Risk, contemp</b>	$\sigma_\sigma$	13.94	5.07	20.58	0.97	1.39	0.76
<b>Signals on risk</b>	$\sigma_{\sigma^{\text{signal}}}$	68.29	44.23	75.90	6.79	5.98	6.20
<b>Risk and signals</b>	$\sigma_\sigma$ and $\sigma_{\sigma^{\text{signal}}}$	82.22	49.30	96.48	7.76	7.38	6.96
<b>all shocks</b>		100.00	100.00	100.00	100.00	100.00	100.00

Signal matters!



# Importance of Risk Signals

News Specification on Risk and Marginal Likelihood (EA data)

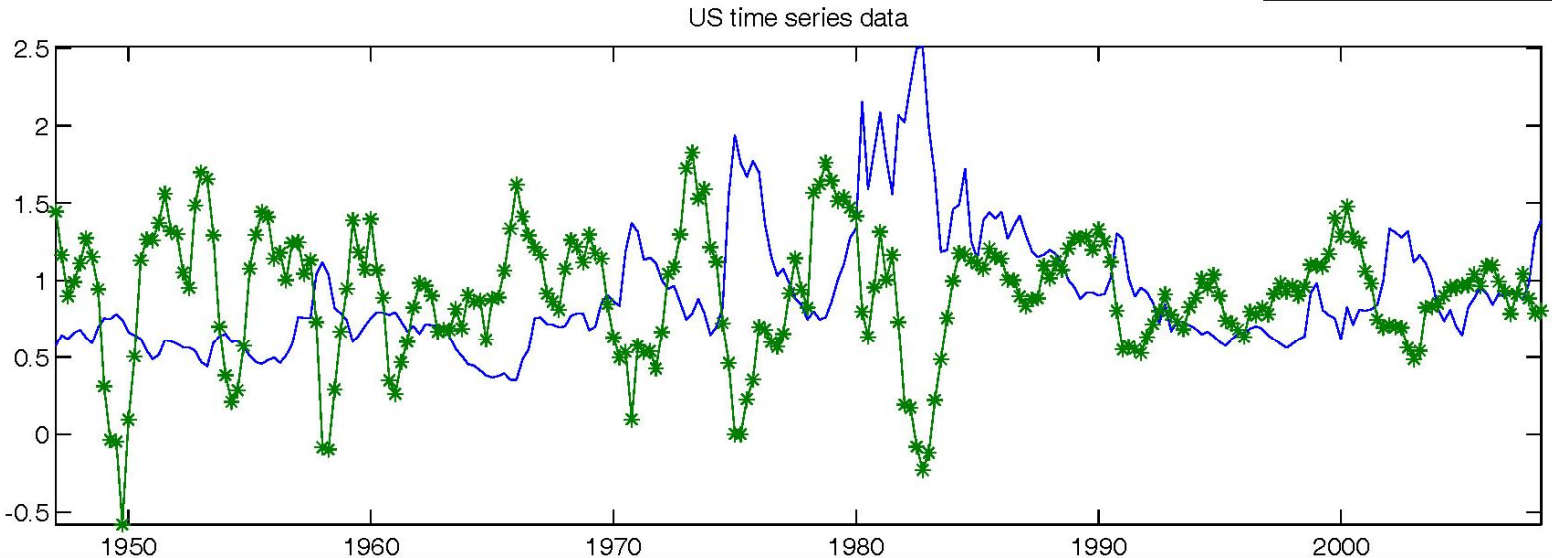
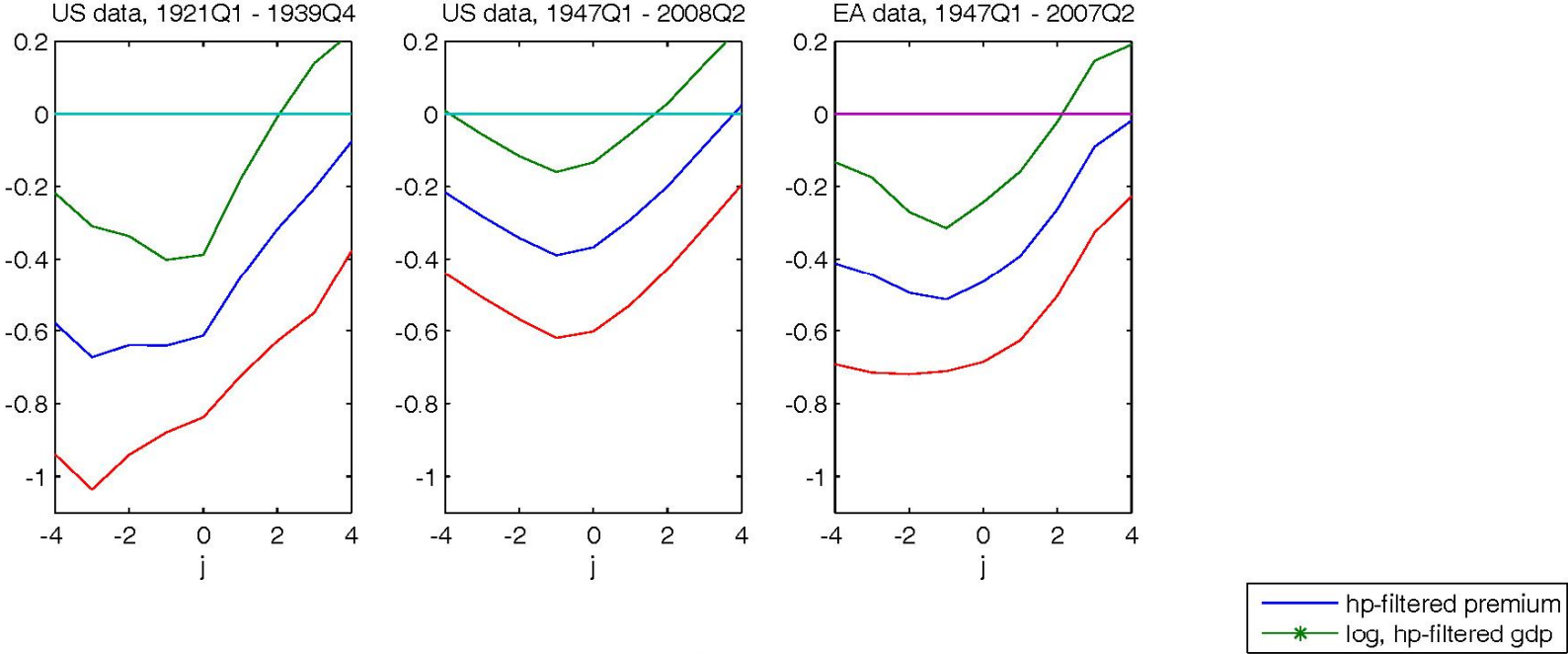
$$\hat{\sigma}_t = \rho_1 \hat{\sigma}_{t-1} + \xi_{t-0}^0 + \xi_{t-1}^1 + \xi_{t-2}^2 + \dots + \xi_{t-p}^p$$

$p$	log, marginal likelihood	odds (=exp(difference in log likelihood from baseline))
8 (baseline)	4397.487	1
6	4394.025	31
1	4325.584	$\infty$

# Why is Risk Shock so Important?

- According to the model, external finance premium is primarily risk shock.
- To look for evidence that risk might be important, look at dynamics of external finance premium and gdp.
- External finance premium is a negative leading indicator

Figure 1: Correlation(finance premium (t),output (t-j)), HP filtered data, 95% confidence interval

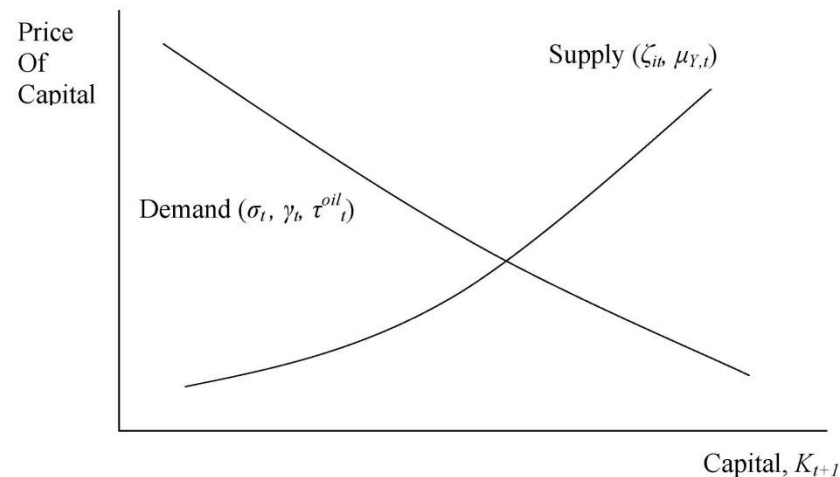


Notes: Premium is measured by the difference between the yield on the lowest rated corporate bonds (Baa) and the highest rated corporate bonds (Aaa). Bond rate data obtained from St. Louis Fed website. GDP data obtained from Balke and Gordon (1986). Filtered output data are scaled so that their standard deviation coincide with that of the premium data.

# Why is Risk Shock so Important?: A second reason

- Our data set includes the stock market
  - Output, stock market, investment all procyclical (surge together in late 1990s)
  - This is predicted by risk shock.

Supply (Capital Producers) and Demand (Entrepreneurs) for Capital





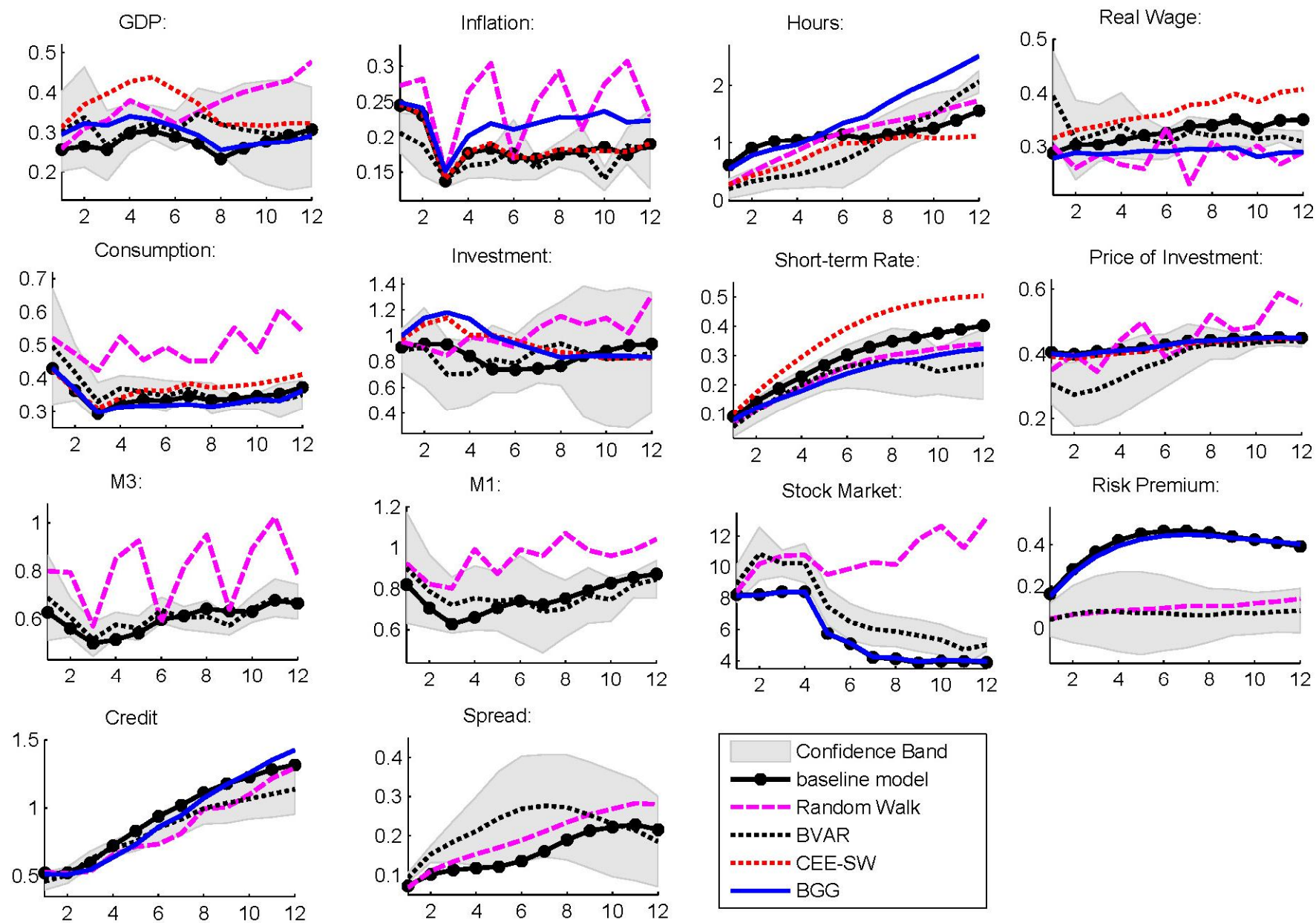
# Impact on Propagation

- Effects of monetary shocks on gdp amplified by BGG financial frictions because  $P$  and  $Y$  go in same direction.
- Effects of technology shocks on gdp mitigated by BGG financial frictions because  $P$  and  $Y$  go in opposite directions.

# Out of Sample RMSEs

- There is not a loss of forecasting power with the additional complications of the model.
- The model does well on everything, except the risk premium.

Figure 6.a. EA, RMSE: Confidence band represents 2 std and is centred around BVAR



# Conclusion

- Incorporating financial frictions changes inference about the sources of shocks and of propagation.
- Models with financial frictions can be used to ask interesting policy questions:
  - When there is an increase in risk spreads, how should monetary policy respond?