# Money and Banking in a New Keynesian Model

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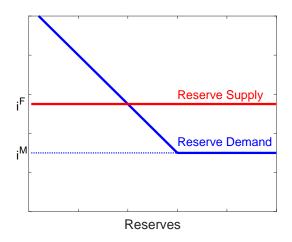
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#### Motivation

- Standard New Keynesian model
  - ► central bank controls short rate in household stochastic discount factor
  - ► short rate = return on savings & investment
- This paper: New Keynesian model with banking sector
  - central bank controls interest rate on fed funds or reserves
  - households do not hold these assets directly
  - banks hold these assets to back inside money
  - $\rightarrow$  disconnect between policy rate & short rate
- Central bank operating procedures:
  - chooses regime/reserve supply: scarce vs ample
  - matters for effectiveness of monetary policy

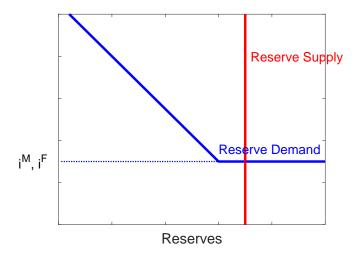
### Corridor system with scarce reserves

- monetary policy targets fedfunds rate, sets reserve rate
- trading desk supplies reserves elastically to meet target
- banks' cost of liquidity > 0, rises if central bank tightens



### Floor system with ample reserves

- monetary policy sets reserve rate & quantity of reserves
- banks' cost of liquidity zero, remains zero if central bank tightens



#### **Implications**

- Standard NK model
  - ▶ interest rate is all that matters, plumbing & quantities not important
- Banking & short rate disconnect: plumbing & quantities matter
  - ► floor system: interest rate policy only affects banks' cost of safety
    - higher reserve rate, cheaper safe collateral to back inside money, lower cost of liquidity for households, not banks, policy weaker
    - quantity of reserves is independent policy tool
  - corridor system: interest rate policy also affects banks' cost of liquidity
    - higher interbank rate, implemented with lower reserves (not indep.)
    - higher cost of liquidity for households & banks, stronger policy
  - both systems
    - less scope for multiple equilibria with short-rate disconnect (savings rate adjusts to inflation even if e.g. policy rate at peg)
    - nominal assets held by banks matter for output & inflation (banks' cost of safety depends on all collateral, not just reserves)

#### Plan for talk

- Transmission in minimal model with disconnect
  - ► Households make payments with CBDC (no banks)
- Introduce banks that provide inside money for payments
  - ► Government supplies ample reserves (floor system)
  - Scarce reserves (corridor system)

#### Literature

- NK models with financial frictions & banking
  - Bernanke-Gertler-Gilchrist 99, Cúrdia-Woodford 10, Gertler-Karadi 11, Gertler-Kiyotaki-Queralto 11, Christiano-Motto-Rostagno 12, Del Negro-Eggertson-Ferrero-Kiyotaki 17, Diba-Loisel 17, Arce-Nuño-Thaler-Thomas 19
- Convenience yields on bonds Patinkin 56, Tobin 61, Bansal-Coleman 96, Krishnamurthy-Vissing-Jorgensen 12, Andolfatto-Williamson 14, Nagel 15, Hagedorn 18, Michaillat-Saez 19
- Convenience yield on assets that back medium of exchange Kiyotaki-Moore 05, Williamson 12, Venkateswaran-Wright 13, Lenel-Piazzesi-Schneider 19
- Bank competition Yankov 12, Driscoll-Judson 13, Brunnermeier-Sannikov 14,
   Duffie-Krishnamurthy 16, Bianchi-Bigio 17, Egan, Hortacsu-Matvos 17,
   Drechsler-Savov-Schnabl 17, DiTella-Kurlat 17
- Recent work on dynamics of the New Keynesian model at ZLB information frictions, bounded rationality, fiscal theory, incomplete markets

# Minimal model with short rate disconnect (no banks)

- Representative household
  - ► utility separable in labor + CES bundle of consumption & money
  - $\bullet$   $\sigma = IES$  for bundles,  $\eta = interest$  elasticity of money demand
  - lacktriangleright for now, separable in consumption & money:  $\eta=\sigma$
  - later consider complementarity:  $\eta < \sigma$
- Firms
  - ► consumption goods = CES aggregate of intermediates
  - ► intermediate goods made 1-1 from labor, Calvo price setting
- Government: central bank digital currency
  - ▶ path or feedback rule for money supply D<sub>t</sub>
  - path or feedback rule for *policy rate*  $i_t^D$  = interest rate on money
  - ► lump sum taxes adjust to satisfy budget constraint
- Market clearing: goods, money, labor
  - $ightharpoonup i_t^S = ext{short rate in household SDF adjusts endogenously}$

### Linear dynamics

- Steady state with zero inflation
- Standard NK Phillips curve & Euler equation,  $\kappa = \lambda \left( \varphi + \frac{1}{\sigma} \right)$

$$\begin{split} \Delta \hat{\rho}_t &= \beta \Delta \hat{\rho}_{t+1} + \kappa \hat{y}_t \\ \hat{y}_t &= \hat{y}_{t+1} - \sigma \left( i_t^S - \Delta \hat{\rho}_{t+1} - \delta \right) \end{split}$$

Households' money demand

$$\hat{d}_t - \hat{p}_t = \hat{y}_t - \frac{\eta}{\delta - r^D} \left( i_t^S - i_t^D - \left( \delta - r^D \right) \right)$$

Why money does not matter in the standard NK model

$$\begin{split} \Delta \hat{\rho}_t &= \beta \Delta \hat{\rho}_{t+1} + \kappa \hat{y}_t \\ \hat{y}_t &= \hat{y}_{t+1} - \sigma \left( i_t^S - \Delta \hat{\rho}_{t+1} - \delta \right) \\ \hat{d}_t - \hat{\rho}_t &= \hat{y}_t - \frac{\eta}{\delta - r^D} \left( i_t^S - i_t^D - \left( \delta - r^D \right) \right) \end{split}$$

- Solve for  $(\hat{p}_t, \hat{y}_t, i_t^S, i_t^D, \hat{d}_t)$  given initial condition  $\hat{p}_0$
- Standard model
  - ▶ add 2 policy rules: Taylor rule for  $i_t^S$ , peg for  $i_t^D = 0$
  - ightharpoonup quantity of money  $\hat{d}_t$  endogenous, adjusts to implement policy rule
  - $\rightarrow$  policy rate = short rate
    - ▶ money does not matter, system is block recursive: solve for  $(\hat{p}_t, \hat{y}_t)$  given  $i_t^S$ ,  $i_t^D = 0$  and initial condition  $\hat{p}_0$

# Why money matters in CBDC model

$$\begin{split} \Delta \hat{\rho}_t &= \beta \Delta \hat{\rho}_{t+1} + \kappa \hat{y}_t \\ \hat{y}_t &= \hat{y}_{t+1} - \sigma \left( i_t^S - \Delta \hat{\rho}_{t+1} - \delta \right) \\ \hat{d}_t - \hat{\rho}_t &= \hat{y}_t - \frac{\eta}{\delta - r^D} \left( i_t^S - i_t^D - \left( \delta - r^D \right) \right) \end{split}$$

- CBDC model
  - ▶ adds 2 policy rules: interest on money  $i_t^D$ , quantity of money  $D_t$
  - $\blacktriangleright$  short rate  $i_t^D$  endogenous, satisfies Euler equation
  - $\rightarrow$  disconnect: policy rate  $\neq$  short rate
    - ▶ money matters, system no longer block recursive: solve for  $(\hat{p}_t, \hat{y}_t, i_t^S)$  given policy rules  $i_t^D$  and  $D_t$
    - familiar special case: NK model with money growth rule & peg  $i_t^D=0$

### Disconnect and role of money with banks

- standard model: policy rate = short rate, money does not matter
- CBDC model: policy rate ≠ short rate, money matters
- banking model with floor system works like CBDC model
  - ▶ rules for reserve rate  $i_t^M$ , quantity of reserves  $M_t$
  - ► short rate disconnect: households do not hold reserves
- banking model with corridor system
  - rules for fed funds rate  $i_t^F$ , peg for reserve rate  $i_t^M = 0$
  - ▶ reserves endogenously adjust to implement policy rule
    → closer to standard model
  - ▶ but still short rate disconnect: households do not hold fed funds

### Interest rate policy

• Standard model: short rate  $i_t^S = \text{policy rate}$ 

Transmission of interest rate policy

• Money supplied elastically to implement  $i_t^S$ , fix  $i_t^D = 0$ 

# Interest rate policy

CBDC model: convenience yield is endogenous wedge

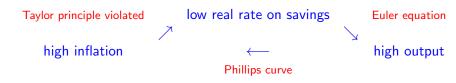
$$i_t^S - \delta = i_t^D - r^D + \frac{\delta - r^D}{\eta} \left( \hat{p}_t + \hat{y}_t - \hat{d}_t \right)$$
 policy rate convenience yield, increasing in velocity = spending / money

Transmission of interest rate policy

⇒ convenience yield dampens effect

### Local determinacy with interest rate peg

- Standard model: many bounded solutions to difference equation
- When do we get multiple bounded equilibrium paths?



- ullet Taylor principle: policy reacts aggressively to high inflation ullet high real rate on savings
- CBDC model: savings rate = policy rate + convenience yield higher convenience yield → higher real rate on savings
- ullet generalized Taylor principle: LR of savings rate to inflation > 1

# When do we get local determinacy with separable utility?

- Taylor rule  $i_t^D = r^D + \phi_\pi \Delta \hat{p}_t + \phi_y \hat{y}_t + v_t$
- Money supply rule  $D_t = \mu D_{t-1} + P_t G$ ,  $\mu \leq 1$ 
  - ightharpoonup choose  $\mu$ , G,  $r^D$  to achieve zero inflation in steady state
  - with  $\mu=1,~G=0 o$  constant money supply, nominal anchor
  - with  $\mu < 1$ , no nominal anchor: continuum of st.st. price levels
- Unique bounded solution iff

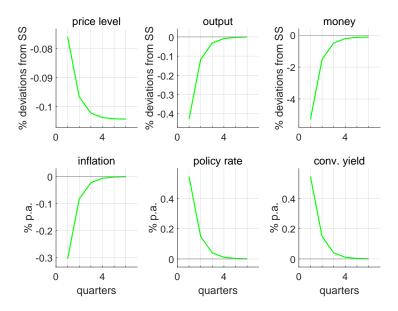
$$LR(i^{S}, \Delta \hat{\rho}) = \frac{\delta - r^{D}}{\eta} \left( \frac{\mu}{1 - \mu} + \frac{1 - \beta}{\kappa} \right) + \phi_{\pi} + \phi_{y} \frac{1 - \beta}{\kappa} > 1$$

- Less scope for multiple equilibria if
  - lower semielasticity of money demand  $\eta/(\delta-r^D)$
  - $\blacktriangleright$  more nominal asset rigidity in balance sheet: higher  $\mu$
  - $\blacktriangleright$  prices more sticky: lower  $\lambda$
  - more aggressive inflation response: higher  $\phi_{\pi}$

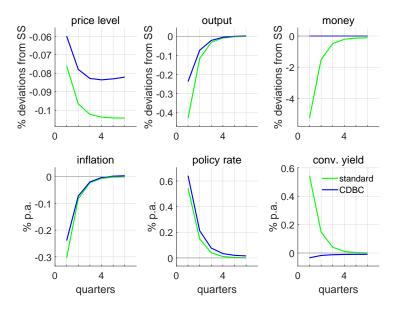
#### Cost channel

- Consumption & money complements in utility
  - ▶ nonseparable utility with  $\eta < \sigma$
  - ▶ higher cost of liquidity  $i_t^S i_t^D$  makes shopping less attractive
    - → reduce consumption, increase leisure/decrease labor
    - $\rightarrow$  lower output, higher inflation
- Effect of higher policy rate on cost of liquidity  $i_t^S i_t^D$ 
  - ▶ standard model: higher  $i_t^S$  with fixed  $i_t^D \rightarrow$  higher cost
  - ullet CBDC model: higher  $i_t^D$  + imperfect pass-through o lower cost
- Numerical example
  - $\delta = 4\%$ ,  $r^D = 1.6\%$ ,  $\sigma = 1$ ,  $\eta = .2$ , standard cost & Calvo pars
  - constant money supply
  - ► Taylor rule with coefficient 1.5 on inflation, .5 on past short rate
  - ► compare impulse responses to 25*bp* monetary policy shock

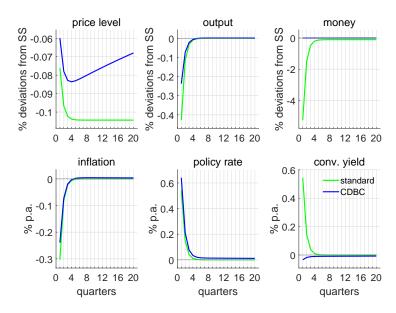
### IRFs to 25 bp monetary policy shock: standard model



### IRFs to 25 bp monetary policy shock: standard vs CBDC

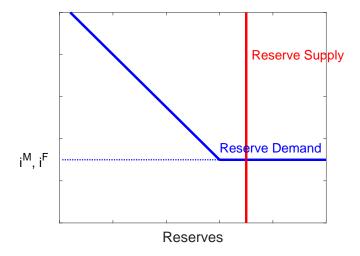


### IRFs to 25 bp monetary policy shock: standard vs CBDC



#### NK Model with Banks

- central bank provides ample reserves ("floor system")
  - ► reserves are special as collateral, not needed for liquidity
  - monetary policy targets reserve rate



### Banking sector

Balance sheet

Assets		Liabilities	
M	Reserves	Money	D
A	Other assets	Equity	

Shareholders maximize present value of cash flows

$$M_{t-1}\left(1+i_{t-1}^{M}\right)-M_{t}+A_{t-1}\left(1+i_{t-1}^{A}\right)-A_{t}-D_{t-1}\left(1+i_{t-1}^{D}\right)+D_{t}$$

- Costless adjustment of equity
- Leverage constraint:  $D_t \le \ell \left( M_t + \rho A_t \right)$ 
  - m 
    ho < 1 other assets are lower quality collateral to back (inside) money

# Bank optimization: perfect competition

- Nominal rate of return on equity =  $i_t^S$ 
  - **b** banks equate returns on assets & liabilities to cost of capital  $i_t^S$
  - $\gamma_t$  = multiplier on leverage constraint
- Optimal portfolio choice: assets valued as collateral

$$i_{t}^{S} = i_{t}^{M} + \ell \gamma_{t} \left( 1 + i_{t}^{S} \right)$$
$$i_{t}^{S} = i_{t}^{A} + \rho \ell \gamma_{t} \left( 1 + i_{t}^{S} \right)$$

Optimal money creation: money requires leverage cost

$$i_t^S = i_t^D + \gamma_t \left( 1 + i_t^S \right)$$

⇒ Marginal cost pricing of liquidity

$$i_t^S - i_t^D = \frac{1}{\ell} \left( i_t^S - i_t^M \right)$$

# Bank market power

- Many monopolistically competitive banks
- Households care about CES bundle of deposit varieties

$$D_t = \left(\int \left(D_t^i
ight)^{1-rac{1}{\eta_b}}
ight)^{rac{1}{1-rac{1}{\eta_b}}}$$

- $\eta_b$  = elasticity of substitution between bank accounts
- ⇒ Constant markup over marginal cost

$$i_t^S - i_t^D = \frac{\eta_b}{\eta_b - 1} \frac{1}{\ell} \left( i_t^S - i_t^M \right)$$

### Equilibrium with ample reserves

- Government: floor system with ample reserves
  - ▶ path or rule for supply of reserves  $M_t$
  - ▶ path or rule for interest rate on reserves  $i_t^M$
- Market clearing for reserves & other bank assets
  - exogenous path  $A_t^r$  of real assets, so  $A_t = P_t A_t^r$
  - ► stands in for borrowing by firms or against housing
- Characterizing equilibrium
  - ► NK Phillips curve & Euler equation unchanged

# Dynamics with ample reserves

Interest rate pass-through: reserve rate to short rate

$$i_t^S - \delta = i_t^M - r^M + \frac{\delta - r^M}{\eta} \left( \hat{p}_t + \hat{y}_t - \hat{d}_t \right)$$

- ► reserves back inside money, inherit convenience yield of deposits
- Money supply

$$\hat{d}_t = \frac{M}{M + \rho A} \hat{\mathbf{m}}_t + \frac{\rho A}{M + \rho A} \hat{a}_t$$

- ► reserves a separate policy instrument: QE stimulates economy!
- other bank assets also matter: bad loan shocks contractionary
- $\Rightarrow$  Works like CBDC model, but coefficients depend on banking system

# Banking with scarce reserves

- Banks manage liquidity
  - deposit outflow/inflow  $\tilde{\lambda}D_t$  to/from other banks
  - ightharpoonup iid liquidity shock  $\tilde{\lambda}$  has mean zero, cdf G with bounded support
  - satisfy leverage constraint after deposit inflow/outflow
  - ightharpoonup borrow/lend in competitive fed funds market at rate  $i^F$
- Assets valued as collateral, reserves also for liquidity
- Government:
  - ▶ path or rule for fed funds rate  $i_t^F$ , reserve rate  $i_t^M$ ; here  $i_t^M = 0$
  - reserve supply adjusts to meet interest rate targets
- Market clearing for reserves, Fed funds
  - ► reserves scarce: quantity small relative to support of liquidity shocks
  - otherwise  $i^F = i^M$  & no active Fed funds market, back to floor
  - ► government selects type of equilibrium

### Dynamics with scarce reserves

Interest rate pass-through: fed funds rate to short rate

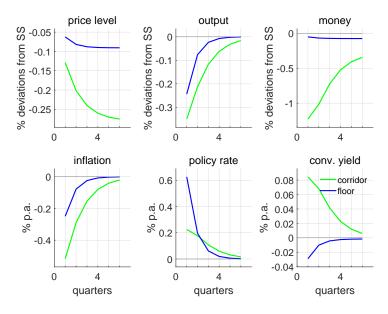
$$i_t^S - \delta = i_t^F - r^M + \frac{\delta - r^M}{\eta} \left( \hat{\rho}_t + \hat{y}_t - \hat{d}_t \right)$$

ullet Inside money in reserveless limit: share of reserves in bank assets o 0

$$\hat{d}_{t} = \frac{\eta}{\eta + \varepsilon} \hat{a}_{t} + \frac{\varepsilon}{\eta + \varepsilon} \left( \hat{p}_{t} + \hat{y}_{t} - \frac{\eta}{r^{F}} \left( i_{t}^{F} - r^{F} \right) \right)$$

- $\varepsilon$  = function of bank technology parameters
- ⇒ Works like CBDC model with more elastic money supply
  - Numerical example to compare floor & corridor system

### 25bp increase in policy rate: corridor vs floor systems



#### Conclusion

- Disconnect between policy rate and short rate
  - convenience yield is endogenous wedge, changes transmission
  - ► less scope for multiple equilibria, even without Taylor principle
  - policy weaker if more nominal rigidities in balance sheets
- Bank models vs CBDC model
  - ► same basic transmission mechanism
  - difference to standard model depends on details of banking system:
    - ★ nominal rigidities in bank balance sheets, bank market power
    - ★ liquidity management & elasticity of deposit supply
- Corridor vs floor system
  - ► with cost channel, significant differences in IRFs
  - corridor system closer to standard model than floor system