

# Scarce, Abundant, or Ample? A Time-Varying Model of the Reserve Demand Curve

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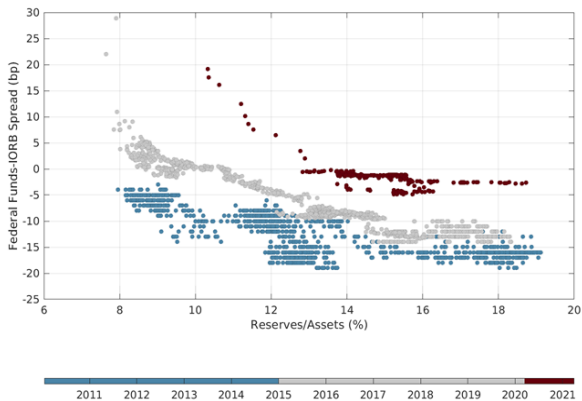
# The Reserve Demand Curve

- ▶ Reserve demand curve:
  - ◇ price at which banks are willing to trade reserves with each other
  - ◇ as a function of aggregate reserves in the banking system
- 1. FOMC communicates stance via range for reserves' lending rates
- 2. Fed can change aggregate reserves, but other factors can too
- ▶ Question: a well-identified, real-time estimate of its slope?

# The FOMC's Ample Reserves Regime

- ▶ *“[T]he Committee reaffirms its intention to implement monetary policy in a regime in which an ample supply of reserves ensures that control over the level of the federal funds rate and other short-term interest rates is exercised primarily through the setting of the Federal Reserve’s administered rates, and in which active management of the supply of reserves is not required.”* (FOMC, October 2019)
  
- ▶ *“Over time, the Committee intends to maintain securities holdings in amounts needed to implement monetary policy efficiently and effectively in its ample reserves regime.”* (FOMC, January 2022)

# Demand for Reserves: Data



# This Paper Estimates Reserve Demand Curve in 2010-2021

- ▶ Three main challenges:

- ◇ nonlinear relationship between prices and quantities
- ◇ unobserved structural changes  $\Rightarrow$  low-frequency movements
- ◇ endogeneity of reserves supply

- ▶ Our approach:

time-varying structural (IV) estimation of price sensitivity with daily data

# Key Results

- ▶ Time-varying estimates of demand elasticity:
  - ◇ Large elasticity → “scarce” reserves (2010, 2019)
  - ◇ Near-zero elasticity → “abundant” reserves (2012-2017, 2020-now)
  - ◇ Intermediate elasticity → “ample” reserves (2011, 2018)
  
- ▶ Ample-to-abundant transition: reserves  $\sim$  12-13% of bank assets
  
- ▶ Demand curve has shifted to the right and upward over time

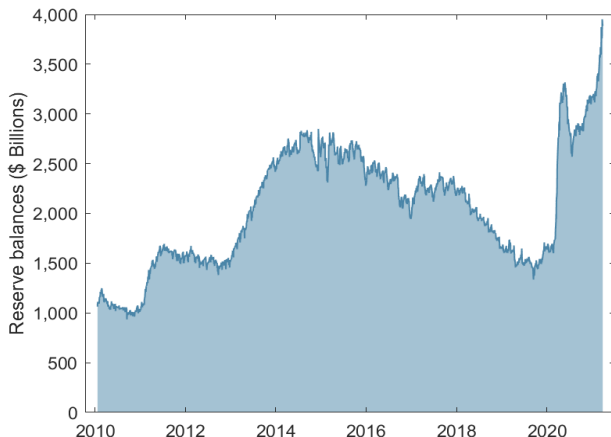
# Outline

1. **Institutional background**
2. Model & Identification Strategy
3. OOS Forecast Evaluation (if time permits)
4. Results

# Reserves in the U.S. Banking System, 2010-21

Long Sample ▷

- ▶ Reserves: deposits held by banks at the Fed

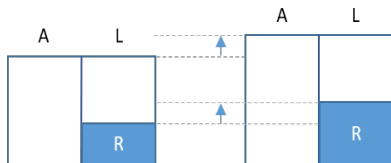


- ▶ Billions before 2008 (GFC) → trillions after 2008

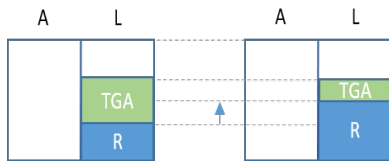


# How Do Reserves Change? Two Ways

- ▶ Reserves: assets for the banks, liability for the Fed



Size of Fed's balance sheet changes



Composition of Fed's liabilities changes

- ▶ Left: Fed expands balance sheet → reserves increase
- ▶ Right: another Fed's liability decreases → reserves increase

# Non-Reserve Liabilities

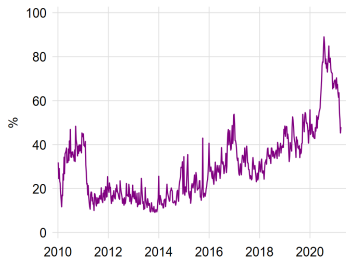
- ▶ Reserves are not a closed system:
  - ◇ banks transact with holders of non-reserve Fed liabilities

Two important examples:

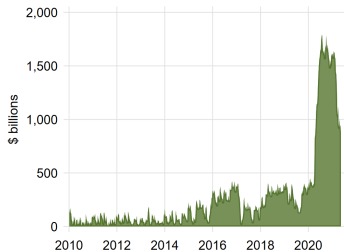
1. Treasury General Account (TGA)
2. Overnight Reverse Repo Facility (ONRRP)

# The Growth of Non-Reserve Liabilities

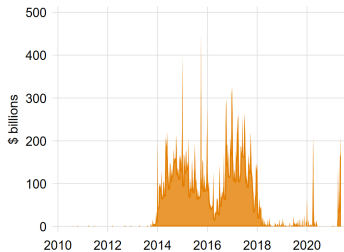
Up to Oct 2022 ▷



Non-Reserves/Reserves



TGA

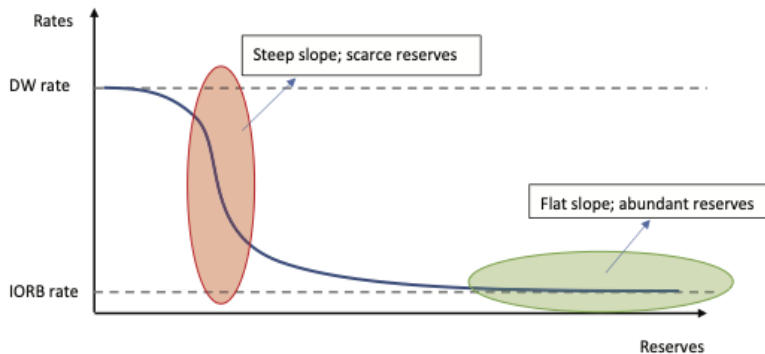


ONRRP

# The Federal Funds Market

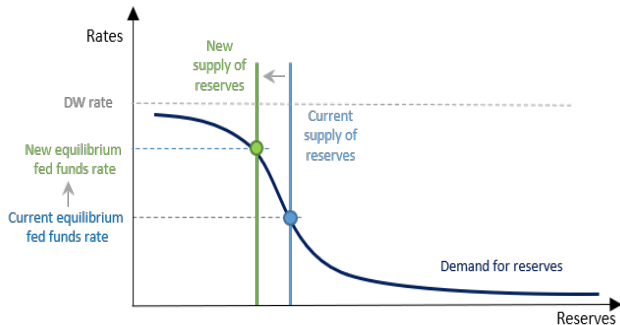
- ▶ “Banks” trade reserves in the federal funds market
  - ◇ unsecured lending (mainly overnight)
  
- ▶ Absent frictions, the federal funds rate should be:
  - ◇ above interest on reserve balances (IORB)
  - ◇ below discount window (DW) rate

# Reserve Demand Curve: Theory



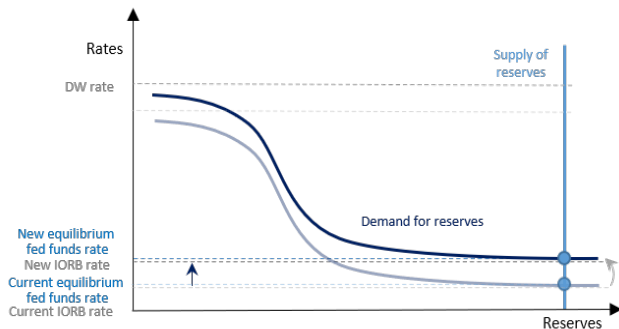
- ▶ Between “scarce” and “abundant” → “ample” reserves

# Monetary Policy Pre 2008



- ▶ Reserves: billions & not remunerated ( $IORB = 0$ )  $\Rightarrow$  steep curve
- ▶ Fed hits target rate by adjusting reserve supply

# Monetary Policy Post 2008



- ▶ Reserves: trillions & IORB  $> 0 \Rightarrow$  flat curve
- ▶ Fed changes IORB (and DW) rate to hit target range

# Two Important Frictions

1. Market segmentation: main money-market lenders do not earn IORB

- ◇ Federal Home Lending Banks (FHLB): federal funds;
- ◇ Money Market Funds (MMF): Eurodollar, repos

2. Banks' balance-sheet constraints:

- ◇ Banks are unwilling to borrow if rate is not sufficiently lower than IORB

⇒ EFR can print below IORB

▶ 2013: Fed introduced ON RRP for FHLBs & MMFs → floor on rates

ONRRP▷



# Low-Frequency Drivers of Reserve Demand Post 2008

- ▶ Liquidity regulation and internal liquidity-risk management
  - ◇ Examples: Liquidity Coverage Ratio (LCR), thin late-day funding market
- ▶ Banks' balance-sheet costs (size-based)
  - ◇ Examples: Supplementary Leverage Ratio (SLR), Federal Deposit Insurance (FDIC) fee
- ▶ Lenders' bargaining power
  - ◇ Example: Federal Home Lending Banks (FHLB) & MMFs' outside option (eg, ONRRP)

# Outline

1. Institutional background
2. **Model & Identification Strategy**
3. OOS Forecast Evaluation (if time permits)
4. Results

## Reserve Demand Curve: Theory

- ▶ Non-linear reserve demand curve with vertical and horizontal shifts:

$$p_t = p_t^* + f(q_t - q_t^*; \theta) + \epsilon_t$$

- ◇  $p_t$ : spread between federal funds rate and IORB
- ◇  $q_t$ : ratio of aggregate reserves to bank assets
- ◇  $p_t^*$ : vertical location (curve's lower bound)
- ◇  $q_t^*$ : horizontal location
- ◇  $f(\cdot; \theta)$  decreasing nonlinear function, parameterized by time-invariant  $\theta$

# Estimating the Slope of the Reserve Demand Curve

- ▶ Structural demand curve at daily frequency:

$$p_t = \alpha_t + \beta_t q_t + \sigma_t v_t$$

- ◇  $p_t$ : spread between federal funds rate and IORB
  - ◇  $q_t$ : ratio of aggregate reserves to bank assets
  - ◇  $\beta_t$ : elasticity of reserve demand (slope)
- 
- ▶ Idea: time-varying parameters capture non-linearity & low-frequency shifts
  
  - ▶ Assumption: parameters move more slowly than daily demand shocks ( $v_t$ )

## First Type of Endogeneity: Fed's Interventions

- ▶ Fed adjusts reserve supply in response to unusual price dislocations
  - ◇ Examples: September 2019, March 2020
  
- ▶ Response is quick but with delay of at least one day
  
- ▶ Prices respond quickly returning to prior level within days

## Second Type of Endogeneity: Non-Reserve Liabilities

1. Changes in non-reserve liabilities mechanically affect level of reserves
  2. They can also correlate with reserve-demand shocks!
- ▶ Non-reserve liabilities are used by key money-market participants
    - ◊ Treasury (TGA), MMFs (ONRRP), FHLBs (ONRRP, Fed accounts)
  - ▶ September 2019 (repo-market spillover), 2021-2022 (ONRRP take-up)

## Example: Banks' Window-dressing

- ▶ Month-ends: European banks reduce wholesale short-term borrowing
  - ⇒ Downward pressure on reserve demand
  
- ▶ MMFs place more cash at ONRRP
  - ⇒ Reserves decrease
  
- ▶ Window-dressing of European banks reverts within few days

## Example: Treasury Auctions

- ▶ Settlement dates: banks' demand for overnight funding increases
  - ⇒ Upward pressure on reserve demand
  
- ▶ Banks send reserves to the Treasury (TGA) for the securities
  - ⇒ Reserves decrease
  
- ▶ Transient but frequent confounding factor
  - ◇ Similar: corporate tax payments



# Estimation: Instrumental Variables (IV) Approach

1. Forecasting model of joint dynamics of reserves ( $q$ ) and rates ( $p$ )
  - ◇ Time-varying VAR with stochastic volatility
  - ◇ Daily data; 10 lags
  - ◇ Bayesian estimation
  - ◇ Coefficients follow random walk slower than daily shocks
  - ◇ Good out-of-sample (OOS) accuracy
2. Five-day-ahead reserves' forecast errors as instrument
3. Estimated  $\widehat{\beta}_t^{(IV)}$  derived from Bayesian estimation of TV-VAR

# Our IV Methodology

- ▶ Estimate TV-VAR  $\rightarrow$  reserves' forecast errors  $u_{q,t} = q_t - q_{t|t-1}$
- ▶ Use error  $u_{q,t-5}$  as instrument for  $q_t$  in structural equation:

$$s_t = \alpha_t + \beta_t q_t + \sigma_t v_t$$

$$\Rightarrow \text{IV estimate: } \widehat{\beta}_t^{(IV)} = \frac{\text{COV}_t(s_t, u_{q,t-5})}{\text{COV}_t(q_t, u_{q,t-5})}$$

- ▶ Instead of usual 2SLS, pull back  $\text{cov}(\cdot)$  from the inversion of a the reduced-form TV-VAR:

$$\Rightarrow \widehat{\beta}_t^{(IV)} = \frac{\text{GIRF}_{t,5} \text{ of rates to reserve}}{\text{GIRF}_{t,5} \text{ of reserves to reserve}} \left( \frac{\text{'reduced-form'}}{\text{'first-stage'}} \right)$$

## Our IV Methodology in Detail (I)

- ▶ The forecasting model: time-varying vector autoregressive (TV-VAR) model with stochastic volatility (Primiceri, 2004):

$$q_t = c_{q,t} + b_{q,q,1,t}q_{t-1} + b_{q,p,1,t}p_{t-1} + \dots + b_{q,q,m,t}q_{t-m} + b_{q,p,m,t}p_{t-m} + u_{q,t},$$

$$p_t = c_{p,t} + b_{p,q,1,t}q_{t-1} + b_{p,p,1,t}p_{t-1} + \dots + b_{p,q,m,t}q_{t-m} + b_{p,p,m,t}p_{t-m} + u_{p,t},$$

- ▶ The  $u$ 's are the forecast errors.

$$(u_{q,t}, u_{p,t})' \sim \mathcal{N}(0, \Omega_t)$$

## Our IV Methodology in Detail (II)

- ▶ Instead of usual IV estimation (2SLS)
- ▶ We directly pull back IV covariances from reduced-form VAR's estimation

$$q_t = \sum_{j=1}^{\infty} \psi_{q,q,j,t} u_{q,t-j} + \tilde{q}_t \quad \& \quad s_t = \sum_{j=1}^{\infty} \psi_{s,q,j,t} u_{q,t-j} + \tilde{s}_t$$

$\psi_{q,q,\cdot}$  &  $\psi_{s,q,\cdot}$ : GIRFs of reserves and rates to reserves  
IRFs of reserves and rates to reserves shocks with recursive identification  
( $q_t$  ordered first)

$\tilde{q}_t, \tilde{s}_t$ : linear combinations of rates' forecast errors  $u_{s,t}$

- ▶ Estimate VAR so that  $u_s$  are residualized wrt  $u_q$
- ▶ Our IV estimate of rate elasticity to reserves:  $\beta_t = \frac{\psi_{s,q,h,t}}{\psi_{q,q,h,t}}$

## Exogeneity of Our Instrument: Daily Data Are Key

- ▶ Exclusion restriction:  $u_{q,t-5}$  uncorrelated with  $v_t$  (demand's error)
  1. Fed's response to price dislocations has a delay of at least a day
    - ◇ And prices normalize quickly
  2. Confounding factors via non-reserve liabilities last less than 5 days
    - ◇ Examples: Treasury auctions & tax payments

# Relevance of Our Instrument

1. Persistence of reserves' path in our sample
2. Forecasting accuracy of our model (even OOS)



- ▶ 5-day-ahead reserve-to-reserve IRF: significant throughout sample
  - ◇ equivalent of first-stage in traditional IV

## Advantages & Robustness

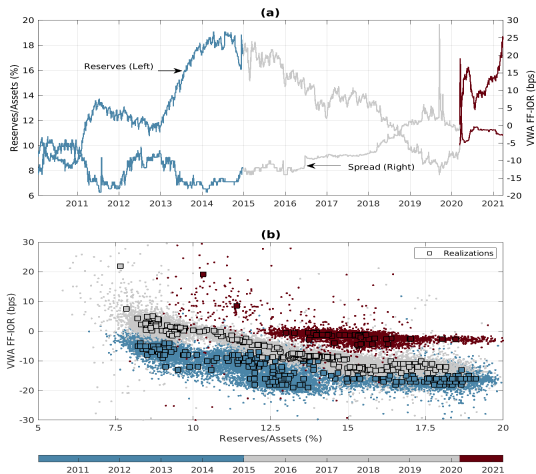
- ▶ Automatically robust to weak instruments (vs ordinary 2SLS)
  - ◇  $\beta$ 's posterior already reflects uncertainty in denominator IRF
- ▶ Robust to autocorrelation & heteroskedasticity
  - ◇ Ratio of IRFs estimated from VAR with 10 lags & stochastic volatility
- ▶ Robustness checks:
  - ◇ Add confounders to forecasting model (repo, T-bill, MMF rates)
  - ◇ Change reserves' normalization (GDP, bank deposits)

# Outline

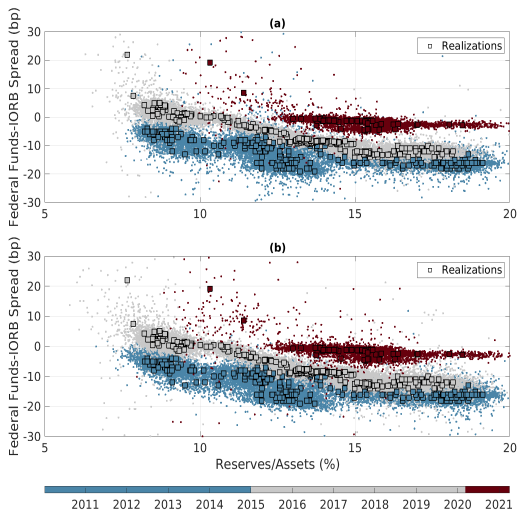
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3. **Results**



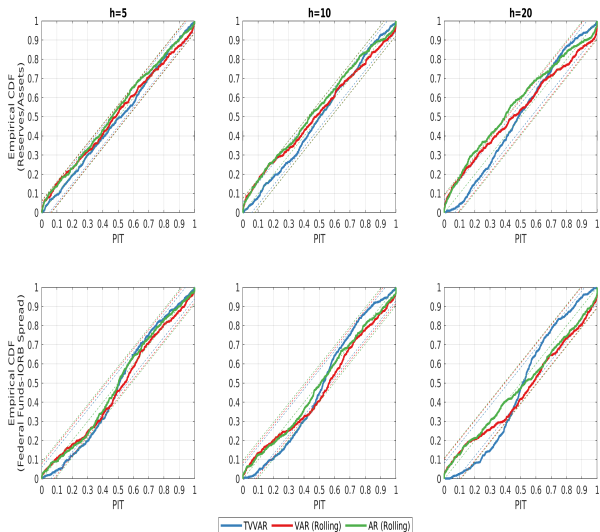
# Out-of-Sample (OOS) Forecasting Accuracy



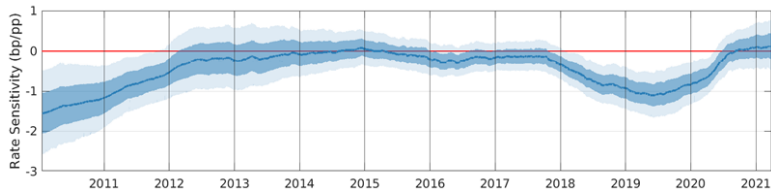
# Out-of-Sample (OOS) vs In-Sample (IS)



# Calibration



# Estimated Slope of the Reserve Demand Curve



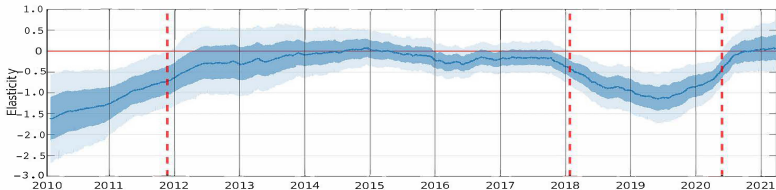
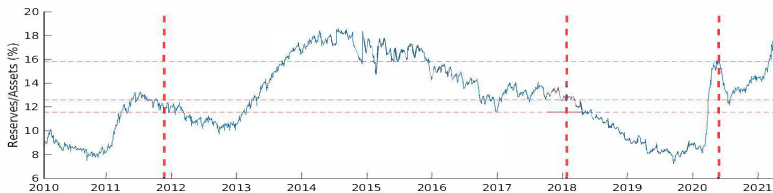
- ▶ Statistically significant negative slope in 2010-2011 and in 2018-2020H1
- ▶ Near-zero slope during 2012-17 and 2020H2-2021Q1

IRFs >

Oct 2022 >

# From Abundant (Flat) to Ample (Gently Sloped)?

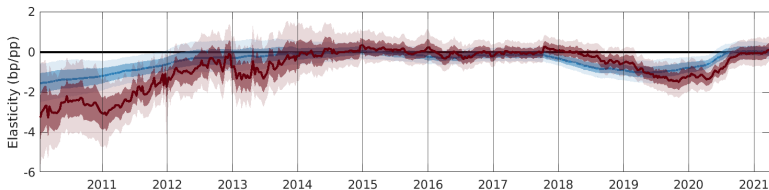
- ▶ Slope emerges around 12% of bank assets in 2011 and 13% in 2018
- ◊ Reserves = \$1.6tn in 2011 and \$2.2tn in 2018



# Real-time Monitoring of Reserve Ampleness

OOS IV estimate: expanding windows every 5 days

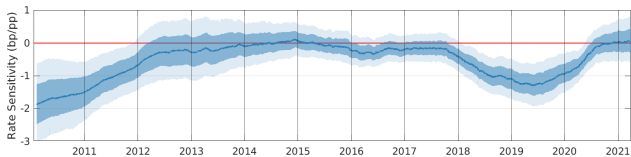
- ▶ Close to IS estimates
- ▶ Becomes significant in 2018Q3-2019Q1 (12-6 months before Sept 2019)



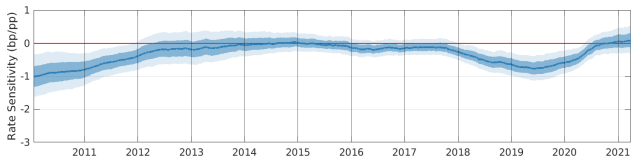
Up to Oct 2022 ▾

# Robustness: Different Reserve Normalizations

## ► Normalizing reserves by GDP

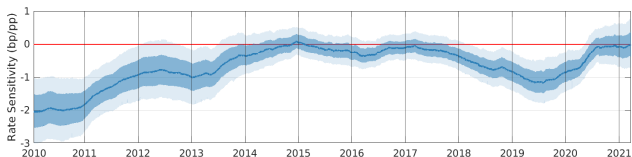


## ► Normalizing reserves by bank deposits

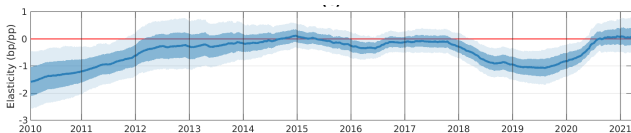


# Robustness: Controlling for Other Market Rates

- ▶ Adding repo rates in TV-VAR (trivariate)



- ▶ Adding T-bill yields in TV-VAR (trivariate)



- ▶ Same with MMF rates



# Quantifying Horizontal and Vertical Shifts in Demand

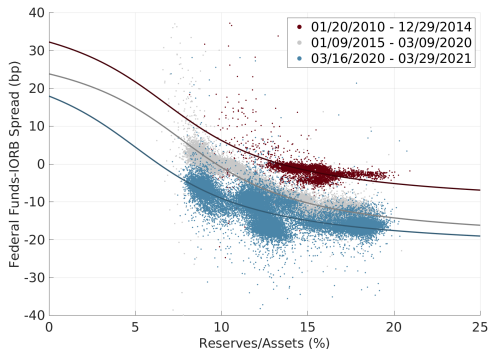
- ▶ Specify non-linear functional form with vertical & horizontal shifts
  - ◊ Only 3 periods for simplicity (but daily varying also possible)
- ▶ Non-linear fit on draws from time-varying forecasting model:

$$\hat{p}_{i,t} = p_t^* + f(\hat{q}_{i,t} - q_t^*; \theta) + e_{i,t}$$

$$f(x; \theta) = \left( \arctan \left( \frac{\theta_1 - x}{\theta_2} \right) + \frac{\pi}{2} \right) \theta_3$$

- ◊  $\hat{p}_{i,t}$  and  $\hat{q}_{i,t}$ : forecast draws ( $i = 1, \dots, N$  for each  $t$ )
- ◊  $p_t^*$ : vertical location (curve's lower bound)
- ◊  $q_t^*$ : horizontal location

# Post-processing Non-linear Fit on Model Forecasts



▶ Horizontal shift to the right: 1-2 percentage points

▶ Vertical shift upward: 12-13 basis points

⇒ Spread by itself is not a reliable summary statistic of rate sensitivity

# Possible Drivers of Horizontal and Vertical Shifts

## ▶ Horizontal shifts:

- ◇ Post-crisis liquidity regulation
- ◇ Post-crisis changes in internal liquidity-risk management
- ◇ Precautionary demand due to lack of depth in late-day market

## ▶ Vertical shifts:

- ◇ Bargaining power of key lenders such as FHLBs & MMFs
- ◇ Variation in banks' balance-sheet costs

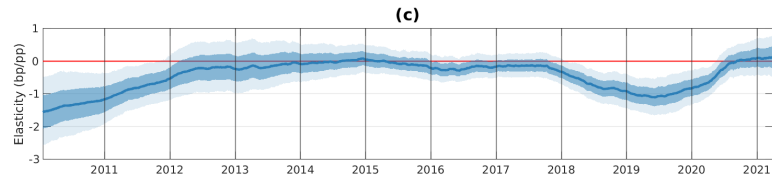
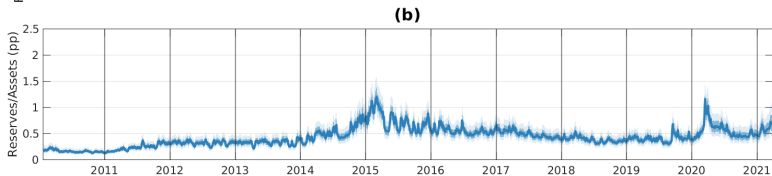
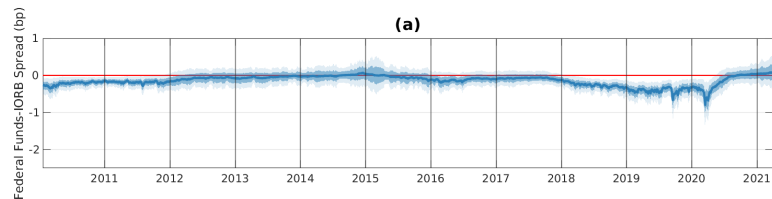
## From Ample (Gently) to Scarce (Steeply Sloped)?

- ▶ Non-linear post-processing fit allows to look at ample-to-scarce transition
  - ◇ IV structural estimates can't because they are locally linear
  
- ▶ Point of maximum slope growth ( $\theta_1 + \theta_2/\sqrt{3}$ ):
  - ◇ Slope changes from gentle to steep
  - ◇ 8-10% pre 2015 & 10-12% post 2015

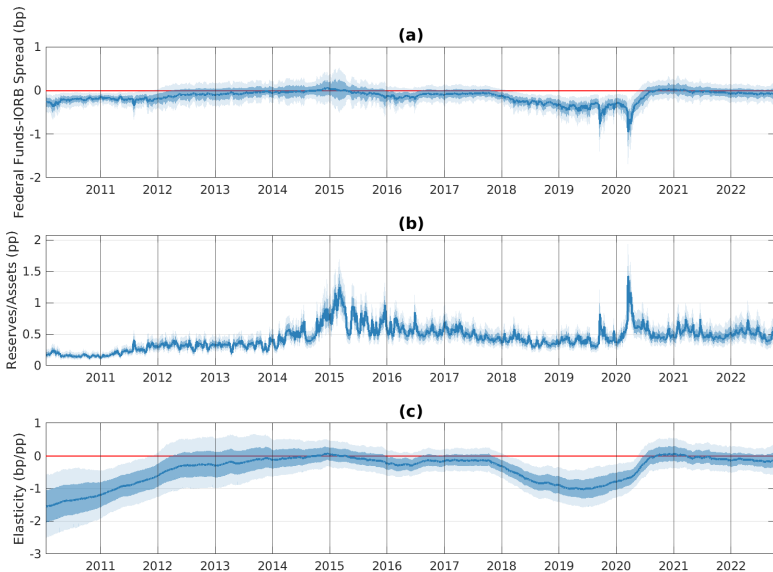
# Conclusions

- ▶ Methodology to identify abundant, ample, and scarce reserves in real time
- ▶ Time-varying estimates of demand elasticity:
  - ◇ Large elasticity → “scarce” reserves (2010, 2019)
  - ◇ Near-zero elasticity → “abundant” reserves (2012-2017, 2020-now)
  - ◇ Intermediate elasticity → “ample” reserves (2011, 2018)
- ▶ Ample-to-abundant transition: reserves  $\sim$  12-13% of bank assets
- ▶ Demand curve has shifted to the right and upward over time

# Numerator and Denominator of IV Estimate



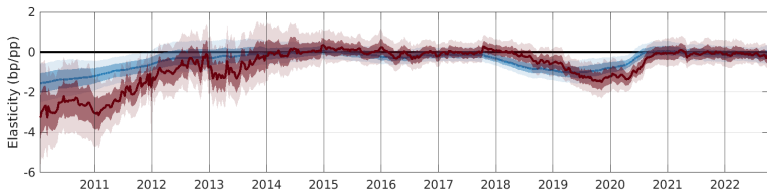
# Estimated Slope Up To October 2022



# Real-time Monitoring of Reserve Ampleness

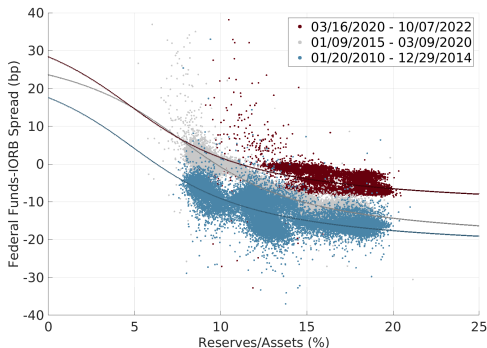
OOS IV estimate: expanding windows every 5 days

- ▶ Close to IS estimates
- ▶ Becomes significant in 2018Q3-2019Q1 (12-6 months before Sept 2019)





# Post-processing Non-linear Fit on Model Forecasts

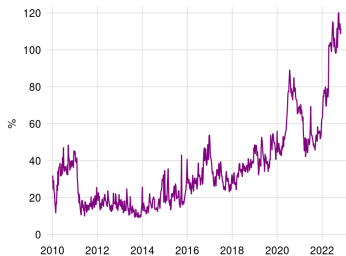


▶ Horizontal shift to the right: 0-2 percentage points

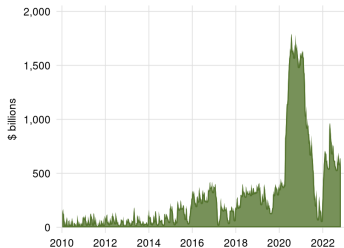
▶ Vertical shift upward: 12-13 basis points

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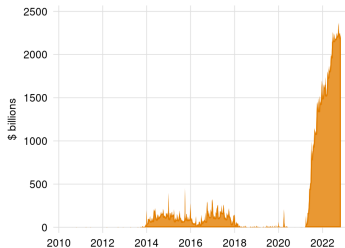
# The Growth of Non-Reserve Liabilities



Non-Reserves/Reserves



TGA



ONRRP

# Overnight Reverse Repo Facility (ON RRP) ◀

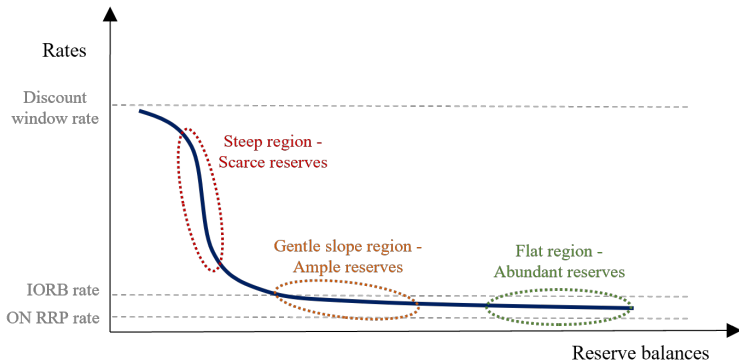


Figure: Reserve demand curve (theory).

- ▶ 2013: Fed introduced ONRRP for FHLBs & MMFs → floor on rates

# Reserves in the U.S. Banking System

