

# Imperfect Information, Macroeconomic Dynamics and the Term Structure of Interest Rates: An Encompassing Macro-Finance Model

Hans Dewachter

KULeuven and RSM, EUR

October 2008

# Overview

- Main goals of the paper
- Motivation
- Macro-Finance framework
- Econometric issues
- Empirical findings
- Conclusions

# Main goals of the paper

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The central question of this paper: Can we improve the existing empirical Macro-Finance models of the yield curve?

Methodological approach:

- Assess/estimate the empirical relevance of three types of extensions of the standard Macro-Finance framework:
  - Deviations from full information rational expectations by introducing learning dynamics (imperfect information).
  - Time variation in the equilibrium real interest rate.
  - Deviations from Gaussian no-arbitrage pricing: time invariant liquidity premiums.
- The empirical analysis is performed using Bayesian techniques combining:
  - Priors consistent with a simple New-Keynesian semi-structural framework.
  - Data on macroeconomic variables, the yield curve and survey data on inflation expectations.

# Motivation

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## A need for more elaborated Macro-Finance models?

Motivation: Despite the long-standing postulate and empirical findings of a close link between the yield curve and the macroeconomic factors, no fully satisfactory macroeconomic model of the yield curve exists:

- Standard New-Keynesian models cannot replicate the variation at the long end of the yield curve:
  - Long-term yields display excessive variation relative to standard NK model, e.g. Kozicki and Tinsley (2001).
  - Excess sensitivity of long-term yields to macroeconomic shocks, e.g. Gürkaynak et al. (2005).
- Standard Macro-Finance models introduce a time-varying inflation target (long-run inflation expectations) and fit the yield curve but face an interpretation problem:
  - Excess volatility in the implied long-run inflation expectations relative to surveys or market indicators of inflation expectations (US data).
  - Implied path for the inflation target does not align with the historical record.

# Motivation

A need for more elaborated Macro-Finance models?

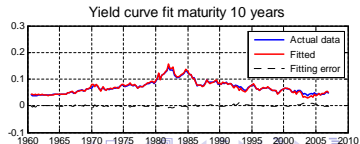
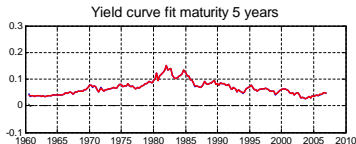
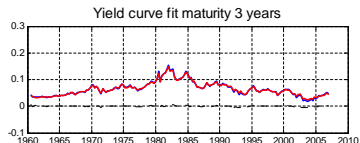
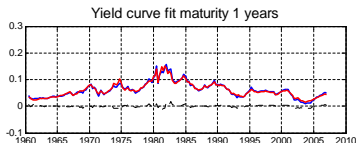
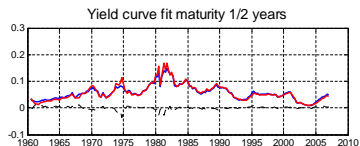
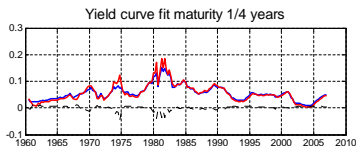
- Performance of the standard NK and Mac-Fin model (US data 1962-2007).

	Yields					Infl. Exp. (SPF)	
Maturity	1/2 yr	1 yr	3yr	5 yr	10 yr	1yr	10yr
Total variation yield (st. dev.)	<b>0.027</b>	<b>0.028</b>	<b>0.027</b>	<b>0.026</b>	<b>0.024</b>	<b>0.020</b>	<b>0.015</b>
	Standard New-Keynesian model						
Residual variation (st. dev.)	<b>0.009</b>	<b>0.009</b>	<b>0.013</b>	<b>0.015</b>	<b>0.018</b>	<b>0.009</b>	<b>0.013</b>
Resid var./total var.	0.333	0.321	0.481	0.577	0.750	0.450	0.867
	Standard Macro-Finance model						
Residual variation (st. dev.)	<b>0.007</b>	<b>0.005</b>	<b>0.002</b>	<b>0.001</b>	<b>0.004</b>	<b>0.008</b>	<b>0.017</b>
Resid var./total var	0.267	0.178	0.074	0.038	0.166	0.400	1.067
	Pure finance model (3 factor Vasicek)						
Residual variation (st. dev.)	<b>0.002</b>	<b>0.002</b>	<b>0.000</b>	<b>0.000</b>	<b>0.002</b>	<b>n.a.</b>	<b>n.a.</b>

# Motivation

A need for more elaborated Macro-Finance models?

- Fit of the US yield curve: standard Mac-Fin model (1960-2007) .

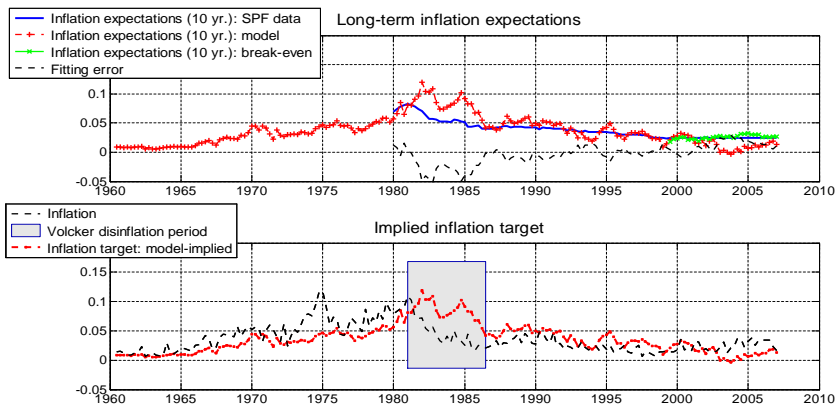




# Motivation

A need for more elaborated Macro-Finance models?

- But (excessively?) volatile implied inflation expectations and target?



# Macro-Finance Framework

## Macro-Finance Framework

# Macro-Finance Framework

## Overview

- The standard Macro-Finance model
- The encompassing model
- Affine yield curve representation
- Perceived Law of Motion
- Learning

# Macro-Finance Framework

## The standard Macro-Finance model

Standard Macro-Finance models (Hordahl et al. (2006), Bekaert et al. (2006), Doh (2006), Dewachter and Lyrio (2006), De Graeve et al. (2007), Rudebusch and Wu (2004)...)

- Extended expectations hypothesis relates the long-term yield,  $y_t(m)$ , to expectations of short-term interest rates,  $E_t(i_{t+j})$ , and maturity-specific risk premiums,  $\varkappa(m)$ :

$$y_t(m) = \frac{1}{m} \sum_{j=0}^{m-1} E_t [i_{t+j}] + \varkappa(m)$$

- Benchmark NK macro model relates interest rate expectations to macroeconomic variables, i.e. inflation, output gap, the policy rate and the inflation target:

$$E_t [i_{t+j}] = f(y_t, (\pi_t - \pi_t^*), i_t, \pi_t^*, j)$$

$$\lim_{j \rightarrow \infty} E_t [i_{t+j}] = \bar{\rho} + \pi_t^*$$

- The yield curve implied by the standard Macro-Finance model is:

$$y_t(m) = \frac{1}{m} \sum_{j=0}^{m-1} f(y_t, (\pi_t - \pi_t^*), i_t, \pi_t^*, j) + \varkappa(m)$$

# Macro-Finance Framework

## The standard Macro-Finance model

### Encompassing/extended Macro-Finance model:

- Extended expectations hypothesis under the Perceived Law of Motion ( $E^P$  PLM):

$$y_t(m) = \frac{1}{m} \sum_{j=0}^{m-1} E_t^P [i_{t+j}] + rp_t$$

- Extended NK macro model including perceived (time-varying) equilibrium real rate,  $\rho_t^P$ :

$$E_t^P [i_{t+j}] = f(y_t, (\pi_t - \pi_t^{*P}), i_t, \pi_t^{*P}, \rho_t^P, j)$$

$$\lim_{j \rightarrow \infty} E_t^P [i_{t+j}] = \pi_t^{*P} + \rho_t^P$$

- The yield curve implied by the extended model (allowing for liquidity effects and time-varying premiums):

$$y_t(m) = \frac{1}{m} \sum_{j=0}^{m-1} f(y_t, (\pi_t - \pi_t^{*P}), i_t, \pi_t^{*P}, \rho_t^P, j) + \varkappa_t(m) + \phi(m)$$

# The Macro-Finance framework

## Affine yield curve representation

We obtain an affine yield curve representation in the (perceived) state,  $X_t^P$  by assuming log-normal pricing (Ang and Piazzesi (2003)):

$$y_t(m) = \underbrace{-a(m)/m - (b(m)/m) X_t^P}_{\text{No-Arbitrage}} + \underbrace{\phi(m)}_{\text{Liq. effect}} + \underbrace{\eta_t(m)}_{\text{meas. err.}}$$

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### No-Arbitrage:

#### PLM dynamics:

$$X_t^P = C^P + \Phi^P X_{t-1}^P + \Gamma^P S^P \varepsilon_t^P$$

#### No-arbitrage conditions:

$$P_t(m) = E_t^P [M_{t,t+1} P_{t+1}(m - 1)]$$

$$M_{t,t+1} = \exp(-i_t - c_m - \Lambda_t' \varepsilon_t^P)$$

$$\Lambda_t = \Lambda_0 + \Lambda_1 X_t^P$$

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### Affine yield curve representation (No-Arbitr.):

$$y_t(m) = -a(m)/m - (b(m)/m) X_t^P$$

### No-arbitrage restrictions:

$$a(m) = a(m - 1) + b(m - 1)(C^P - \Gamma^P S^P S^{P'} \Lambda_0) + JIT$$

$$b(m) = b(m - 1)(\Phi^P - \Gamma^P S^P S^{P'} \Lambda_1) - \delta_1'$$



# The Macro-Finance framework

## Perceived Law of Motion: Macroeconomic dynamics

The Perceived Law of Motion is a VAR(I) in the perceived state,  $X_t^P$  :

$$X_t^P = C^P + \Phi^P X_{t-1}^P + \Gamma^P S^P \varepsilon_t^P, \quad X_t^P = [\pi_t, y_t, i_t, \pi_t^{*P}, \rho_t^P]$$

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New-Keynesian model with stoch. trends  $\pi_t^{*P}$  and  $\rho_t^P$ :

$$\pi_t = \mu_\pi E_t^P \pi_{t+1} + (1 - \mu_\pi) \pi_{t-1} + \kappa y_t + \sigma_\pi \varepsilon_{\pi,t}$$

$$y_t = \mu_y E_t^P y_{t+1} + (1 - \mu_y) y_{t-1} - \phi(i_t - E_t^P \pi_{t+1} - \rho_t^P) + \sigma_y \varepsilon_{y,t}$$

$$i_t = (1 - \gamma_i) i_t^T + \gamma_i i_{t-1} + \sigma_i \varepsilon_{i,t}$$

$$i_t^T = \rho_t^P + E_t^P \pi_{t+1} + \gamma_\pi (\pi_t - \pi_t^{*P}) + \gamma_y y_t$$

$$\pi_t^{*P} = \lim_{s \rightarrow \infty} E_t^P [\pi_{t+s}]$$

$$\rho_t^P = \lim_{s \rightarrow \infty} E_t^P [i_{t+s} - \pi_{t+s}]$$

# The Macro-Finance framework

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$$i_t = (1 - \gamma_i) i_t^T + \gamma_i i_{t-1} + \sigma_i \varepsilon_{i,t}$$

$$i_t^T = \rho_t^P + E_t^P \pi_{t+1} + \gamma_\pi (\pi_t - \pi_t^{*P}) + \gamma_y y_t$$

$$\pi_t^{*P} = \lim_{s \rightarrow \infty} E_t^P [\pi_{t+s}]$$

$$\rho_t^P = \lim_{s \rightarrow \infty} E_t^P [i_{t+s} - \pi_{t+s}]$$

Updating the perceived stochastic trends:

$$\pi_t^{*P} = \pi_{t-1}^{*P} + f(X_t, \dots, X_{t-n})$$

$$\rho_t^P = \rho_{t-1}^P + f(X_t, \dots, X_{t-n})$$

$$X_t = [\pi_t, y_t, i_t, \pi_t^{*P}, \rho_t^P, \pi_t^*, \rho_t]$$

# The Macro-Finance framework

## Learning dynamics

- Learning dynamics are modeled along the lines of Kozicki and Tinsley (2005):

$$\pi_t^P = \pi_{t-1}^{*P} + w_\pi \sigma_{\pi^*} \varepsilon_{\pi^*,t} + (1 - w_\pi) [\sigma_{\pi^b} \eta_{\pi,t} + g_\pi (\pi_t - E_{t-1}^P \pi_t)]$$

$$\rho_t^P = \rho_{t-1}^P + w_\rho \sigma_\rho \varepsilon_{\rho,t} + (1 - w_\rho) [\sigma_{\rho^b} \eta_{\rho,t} + g_\rho (i_t - \pi_t - E_{t-1}^P (i_t - \pi_t))]$$

- The learning rule updates perceived trends in function of three types of information:
  - Actual shocks to the 'true' inflation target and/or equilibrium real rate (e.g. inflation target announcements, release of productivity data, risk perceptions...).
  - Subjective and exogenous belief shocks  $\eta_{\pi^b,t}$ ,  $\eta_{\rho^b,t}$  ( e.g. changes in credibility,...).
  - Subjective and endogenous forecast errors of inflation and real interest rates,  $(\pi_t - E_{t-1}^P \pi_t)$  and  $(i_t - \pi_t - E_{t-1}^P (i_t - \pi_t))$ .
- Although ad hoc, the learning rule embeds as limiting cases:
  - The full info. RE models ( $w_\pi = w_\rho = 1$ ): e.g. stand; Mac-Fin  $\sigma_{\pi^*} \geq 0$ ,  $\sigma_\rho = 0$ .
  - Constant gain learning rule ( $w_\pi = w_\rho = 0$ ,  $\sigma_{\rho^b} = \sigma_{\pi^b} = 0$ ,  $g_\pi > 0$ ,  $g_\rho > 0$ ).

# Econometric issues

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## Overview

- Data
- Summary of Bayesian estimation procedure
  - Sets of estimated parameters
  - Prior distributions
  - Likelihood
- Alternative model versions

# Econometric issues

## Data

Model is estimated on US data: 1960Q2 till 2006Q4.

- Inflation: quarter-by-quarter GDP deflator (p.a. terms) is used. Source: Federal Reserve Economic Data archive (FRED).
- Output gap: CBO output gap measure is used (no- real time data). Source: Congressional Budget Office.
- Policy rate: Fed fund effective rate is used. Source: FRED.
- Yield curve: 1/4, 1/2, 1, 3, 5, 10 yr. maturities. Sources: Gürkaynak et al. (2006) and FRED.
- Inflation expectations: average inflation expectations over 1 and 10 year horizons. Source: Survey of Professional Forecasters, FED Philadelphia.

# Econometric issues

Summary: Bayesian estimation framework

MCMC (Metropolis-Hastings) identification of the posterior density  $p(\theta_i | Z^T)$  :

$$p(\theta_i | Z^T) = L(Z^T | \theta_i)p(\theta_i)/p(Z^T)$$

- Parameters  $\theta_i$ : structural parameters related to the NK model, learning, prices of risk , mispricing and measurement errors.
- Priors of the parameters,  $p(\theta_i)$  :
  - Priors related to structural parameters are in line with macro literature.
  - The priors of the learning model are biased towards rational expectations ( $E(w) = 0.85$ ,  $\sigma(w) = 0.10$ ).
- Likelihood function,  $L(Z^T | \theta_i)$ , generated by the prediction error decomposition (Kalman filter):
  - Transition equation is based on the Actual Law of Motion.
  - Measurement equation combines macroeconomic information  $(\pi_t, y_t, i_t)$ , yield curve variables and inflation expectations surveys.



# Econometric issues

## Versions of the model

**Table:** PROPERTIES OF ALTERNATIVE VERSIONS OF THE MODEL

Model	Macro (# stoch. trends)	Prices of Risk	Expectations	Mispricing	
<b>NK0</b>	NK model (0)	Consistent $\Lambda_0^{IS}$	Full-info RE	Yes	← Stand. NK mod
<b>MF1</b>	NK model (1)	Consistent $\Lambda_0^{IS}$	Full-info RE	Yes	← <b><u>Stand. MF mod</u></b>
<b>MFS</b>	NK model (2)	Consistent: $\Lambda_0^{IS}$	Full-info RE	No	← Struct. MF mod
<b>MFM</b>	NK model (2)	Consistent: $\Lambda_0^{IS}$	Full-info RE	Yes	← Liq. MF mod
<b>MFF</b>	NK model (2)	Free: $\Lambda_0, \Lambda_1$	Full-info RE	No	← Flex. MF mod
<b>MFE</b>	NK model (2)	Free: $\Lambda_0, \Lambda_1$	Learning	Yes	← <b><u>Encompass.mod</u></b>

# Empirical findings

## Empirical findings

# Empirical findings

- Improving standard Macro-Finance models?
  - Comparing model versions
- Estimation results of the MFE model
  - Parameter estimates
  - Implied macroeconomic factors
- Macro factors and the yield curve implied by the MFE model
  - Fit of the yield curve
  - Liquidity effects

# Improving standard Macro-Finance models?

## Comparing model versions

Conclusion 1: The encompassing model, incorporating time-varying equilibrium real rates, imperfect information and liquidity effects, is strongly favored by the data.


**Table:** MODEL PERFORMANCE: MARGINAL LIKELIHOOD AND BIC

Log Marginal likelihood and BIC						
Model	NK0	<b>MF1</b>	MFS	MFM	MFF	<b>MFE</b>
Marg. Lik	6124	<b>7240</b>	7381	7628	7638	<b>7741</b>
BIC	12387	<b>-14591</b>	-14815	-15333	-15384	<b>-15442</b>
Decomposition of BIC						
Model	NK0	<b>MF1</b>	MFS	MFM	MFF	<b>MFE</b>
Macro (-2lnlik)	-3414	<b>-3495</b>	-3760	-3711	-3745	<b>-3772</b>
Yields (-2lnlik)	-7413	<b>-9187</b>	-9037	-9392	-9504	<b>-9538</b>
Infl. exp.(-2lnlik)	-1683	<b>-1447</b>	-2227	-2197	-2182	<b>-2256</b>
Penalty	131	<b>136</b>	131	157	194	<b>272</b>

# Estimation results

## Parameter estimates of the encompassing model

Conclusion 2: The structural parameters of the encompassing model are plausible and aligned to the empirical macro literature.

- The behavioral parameters of the (semi-) structural NK model are in line with empirical macro literature:
  - Relative to benchmark Mac-Fin models, we find stronger forward looking components ( $\mu_\pi = 0.66$ ,  $\mu_y = 0.69$ ). e.g. Galí et al (2005)
    - Phillips curve: low but significant inflation indexation ( $\delta_\pi = 0.53$ ) and output sensitivity ( $\kappa = 0.012$ ).
    - IS-curve: significant habit persistence ( $h = 0.75$ ) and risk aversion in line with macro lit. ( $\sigma = 2.5$ ).
  - Taylor rule parameters in line with the literature. Relatively low interest rate smoothing : ( $\gamma_\pi = 0.4$ ,  $\gamma_y = 0.63$  and  $\gamma_i = 0.69$ ). e.g. Rudebusch (2002).
- Actual stochastic trends:
  - Inflation target displays only small time variation ( $\sigma_{\pi^*} = 0.04\%$ ) but imprecisely estimated.
  - Significant volatility in the equilibrium real rate ( $\sigma_\rho = 0.7\%$ ) but imprecisely estimated. (e.g. Trehan and Wu (2007), Bjornland et al (2006, 2007), Bekaert et al. (2005), Laubach and Williams (2003)...)
 

# Estimation results

## Parameter estimates of the encompassing model

	Param.	Mean	Std. Dev.	Mode	Crit.val. 5%	Crit. val. 95%
Phillips curve						
Inflation indexation →	$\delta_\pi$	0.5337	0.0327	<b>0.5288</b>	0.4829	0.5891
Output sensitivity →	$\kappa$	0.0137	0.0042	<b>0.0117</b>	0.0078	0.0212
IS curve						
Habit persistence →	$h$	0.7512	0.0445	<b>0.7566</b>	0.6741	0.8179
Risk aversion →	$\sigma$	2.6779	0.4004	<b>2.5551</b>	1.9344	3.2328
Monetary policy rule						
Inflation gap →	$\gamma_\pi$	0.3707	0.1081	<b>0.4389</b>	0.2296	0.5824
Output gap →	$\gamma_y$	0.6673	0.1638	<b>0.6341</b>	0.4931	1.0214
Interest smoothing →	$\gamma_i$	0.6827	0.0406	<b>0.6896</b>	0.6462	0.7849
Shocks						
Supply shock	$\sigma_\pi$	0.0118	0.0010	0.0120	0.0101	0.0136
Demand shock	$\sigma_y$	0.0032	0.0003	0.0031	0.0027	0.0038
Policy rate shock	$\sigma_i$	0.0117	0.0007	0.0119	0.0110	0.0131
Inflation target shock →	$\sigma_{\pi^*}$	0.0015	0.0010	<b>0.0004</b>	0.0001	0.0034
Eq. real rate shock →	$\sigma_\rho$	0.0074	0.0014	<b>0.0073</b>	0.0039	0.0083

# Estimation results

## Parameter estimates of the encompassing model

Conclusion 3: Imperfect information and learning effects dominate long-run inflation expectations. The parameter estimates imply only weak anchoring of subjective inflation expectations.

- Inflation belief shocks and adaptive learning effects dominate subjective inflation expectations (at the mode  $w_{\pi^*} = 0.65$ ):
  - Inflation target shocks: **0.03%** ( $w_{\pi} \sigma_{\pi^*} = 0.65 \times 0.04\% = 0.03\%$ ).
  - Inflation belief shocks: **0.20%** ( $(1 - w_{\pi}) \sigma_{\pi^{*b}} = 0.35 \times 0.58\% = 0.20\%$ ).
  - Inflation forecast errors (gain= 0.08) : **0.12%**.
- No strong learning effects observed for the equilibrium real interest rate ( at the mode  $w_{\rho} = 0.97$ ):
  - Real rate (target) shocks: **0.71%** ( $w_{\rho} \sigma_{\pi^*} = 0.97 \times 0.73\% = 0.71\%$ ).
  - Real rate belief shocks: **0.04%** ( $(1 - w_{\rho}) \sigma_{\pi^{*b}} = 0.03 \times 1.2\% = 0.04\%$ ).
  - Real rate forecast errors (gain 0.01): **0.01%**.

# Estimation results

## Parameter estimates of the encompassing model

Table: POSTERIOR DENSITY ESTIMATES IB: LEARNING PARAMETERS

	Param.	Mean	Std. Dev.	Mode	Crit.val. 5%	Crit. val. 95%
Learning parameters: Long-run inflation expectations: $\pi_t^{*P}$						
Weight RE →	$w_\pi$	0.6083	0.0645	<b>0.6550</b>	0.4897	0.6907
Gain →	$g_\pi$	0.2191	0.0255	<b>0.2190</b>	0.1668	0.2479
Belief shock →	$\sigma_{\pi^{*b}}$	0.0045	0.0014	<b>0.0058</b>	0.0015	0.0067
Target shock →	$\sigma_{\pi^*}$	0.0015	0.0010	<b>0.0004</b>	0.0001	0.0034
Learning parameters: perceived eq. real rate: $\rho_t^P$						
Weight RE →	$w_\rho$	0.7789	0.1441	<b>0.9746</b>	0.5858	0.9872
Gain →	$g_\rho$	0.1200	0.0746	<b>0.0443</b>	0.0117	0.2392
Belief shock →	$\sigma_{\rho^b}$	0.0121	0.0058	<b>0.0050</b>	0.0017	0.0194
Eq. real shock →	$\sigma_\rho$	0.0074	0.0014	<b>0.0073</b>	0.0039	0.0083

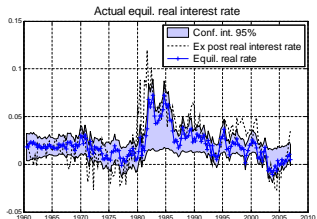
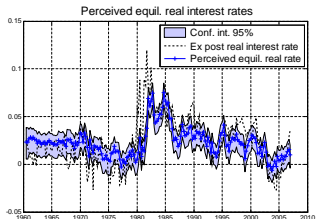
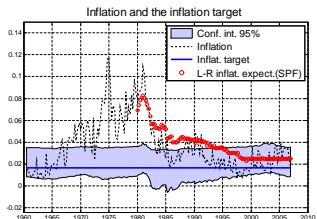
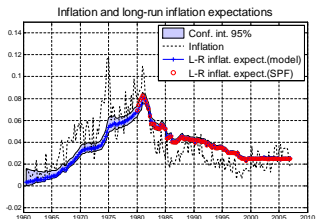
$$\pi_t^{*P} = \pi_{t-1}^{*P} + w_\pi \sigma_{\pi^*} \varepsilon_{\pi^*,t} + (1 - w_\pi) \left[ \sigma_{\pi^b} \eta_{\pi,t} + g_\pi (\pi_t - E_{t-1}^P \pi_t) \right]$$

$$\rho_t^P = \rho_{t-1}^P + w_\rho \sigma_\rho \varepsilon_{\rho,t} + (1 - w_\rho) \left[ \sigma_{\rho^b} \eta_{\rho,t} + g_\rho (i_t - \pi_t - E_{t-1}^P (i_t - \pi_t)) \right]$$



# Estimation results

## Implied factors



# Macro factors and the yield curve

## Yield curve fit

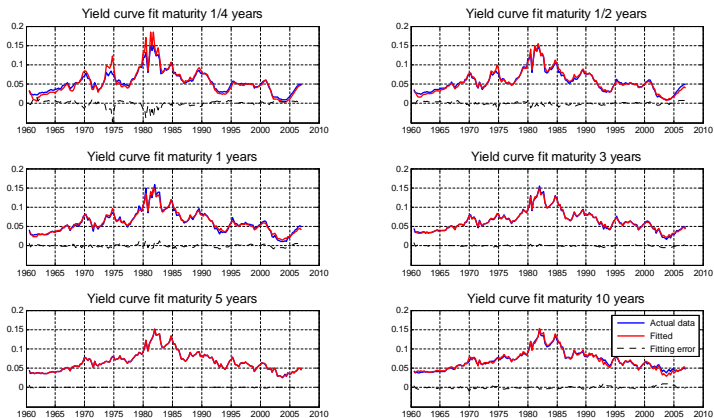
**Conclusion 4:** The encompassing Macro-Finance model captures a substantial part of the time variation of the yield curve and aligns inflation expectations to survey data SPF (unlike standard Mac-Fin models).

	Yields					Infl. Exp. (SPF)	
Maturity	1/2 yr	1 yr	3yr	5 yr	10 yr	1yr	10yr
Total variation yield (st. dev.)	<b>0.027</b>	<b>0.028</b>	<b>0.027</b>	<b>0.026</b>	<b>0.024</b>	<b>0.020</b>	<b>0.015</b>
	Encompassing Macro-Finance model						
Residual variation (st. dev.)	<b>0.005</b>	<b>0.004</b>	<b>0.002</b>	<b>0.001</b>	<b>0.003</b>	<b>0.005</b>	<b>0.001</b>
R-square	0.963	0.979	0.994	0.999	0.978	0.927	0.995
	Standard Macro-Finance model						
Residual variation (st. dev.)	<b>0.007</b>	<b>0.005</b>	<b>0.002</b>	<b>0.001</b>	<b>0.004</b>	<b>0.008</b>	<b>0.017</b>
	Pure finance model (3 factor Vasicek)						
Residual variation (st. dev.)	<b>0.002</b>	<b>0.002</b>	<b>0.000</b>	<b>0.000</b>	<b>0.002</b>	<b>n.a.</b>	<b>n.a.</b>

# Macro factors and the yield curve

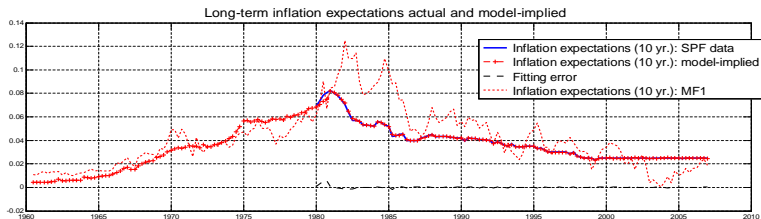
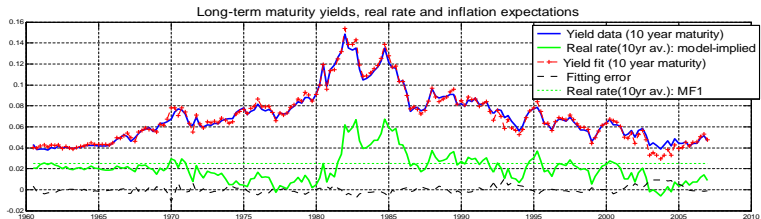
## Yield curve fit

Figure: OBSERVED AND FITTED YIELD CURVE OF THE MFE MODEL



# Macro factors and the yield curve

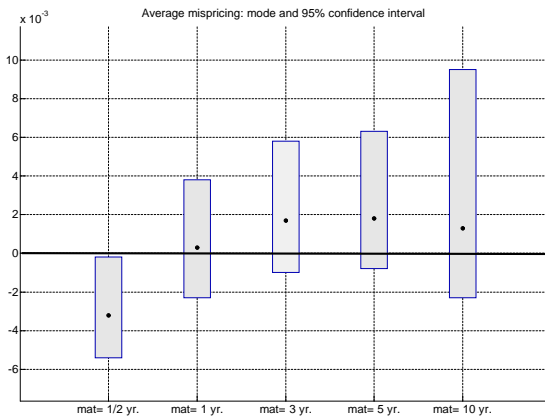
## Yield curve fit



# Macro factors and the yield curve

## Mispricing or liquidity effects

**Conclusion 5:** There is evidence of significant mispricing (liquidity preference effects), especially at the short end of the yield curve.



# Conclusions

- In this paper the standard (empirical) Macro-Finance models are extended by introducing (i) time variation in the equilibrium real interest rate (ii) liquidity effects and (iii) learning.
- The encompassing model outperforms all existing Macro-Finance models. The model 'explains' more than 95% of yield curve dynamics.
- The encompassing model, unlike standard Macro-Finance models, reconciles yield curve dynamics, inflation expectations and the inflation target. The results suggest that:
  - Learning dynamics generate significant differences between long-run inflation expectations and the inflation target. Important drivers of subjective inflation expectations are inflation forecasts errors and belief shocks.
  - Perceived eq. real rate dynamics explain a substantial share of the variation in long-term yields.
  - Significant liquidity and risk premium effects at the short end of the yield curve.
- Open issues:
  - Sources of dynamics in perceived and/or actual equilibrium real interest rate?